

Nonequilibrium Dynamical Mean Field Theory: impurity solver by an auxiliary Master Equation approach

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Institute of Theoretical Physics - Computational Physics

TU Graz

CCQS, Evora, Oct. 2012



Outline of the talk

1 Introduction

2 Model and Method

- Nonequilibrium DMFT
- Impurity solver by an effective quantum Master equation approach

3 Results

4 Summary and Outlook

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Nonequilibrium Strongly Correlated Systems

Systems and materials

- Ultracold atoms
- Transport through heterostructures / quantum dots / spintronics
- Quantum information

Issues

- Nonequilibrium quantum phase transitions
- Decoherence / dissipation
- Thermalisation

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Theoretical approaches

for nonequilibrium strongly correlated systems

- **Perturbative / RG** (Meir et al. 92, Schoeller et al. 94, Rosch et al. 05)
- **Quantum Monte Carlo** (Eckstein et al. (09))
- **Functional Renormalisation Group** (Gezzi, Jakobs et al. (07))
- Bethe Ansatz (Mehta+Andrei 06)
- Numerical Renormalisation Group (Anders 08)
- Density-Matrix RG (White et al. 04, Schollwöck, Heidrich-Meisner, ...)
- Flow equation RG (Kehrein 05)
- **Dynamical Mean-Field Theory** (Schmidt+Monien (02), Freericks, Turkowski, Zlatić (06))
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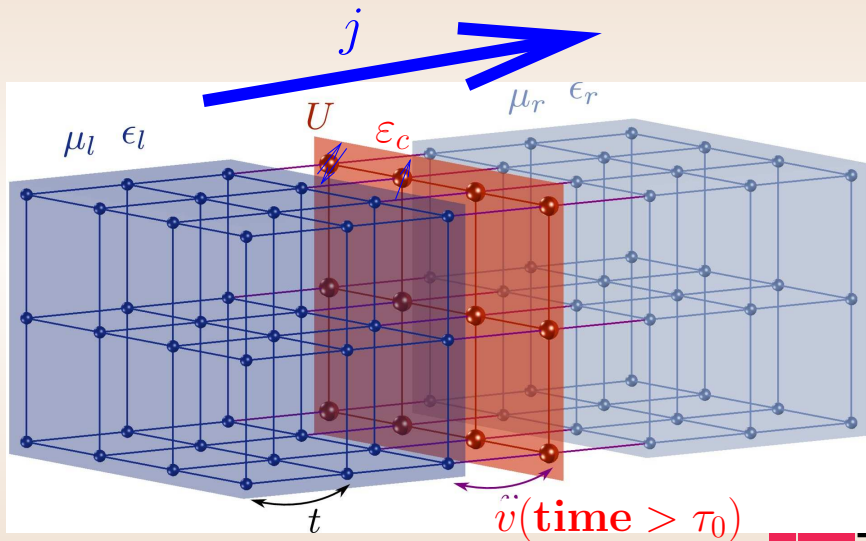
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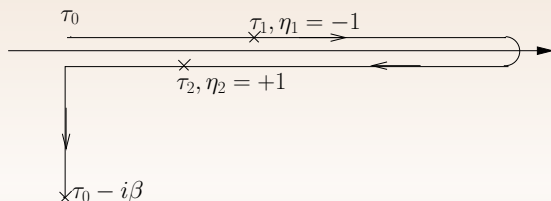
Model



$$\text{Voltage } \phi = \mu_l - \mu_r$$

Nonequilibrium Green's functions

(Kadanoff+Baym, Keldysh, Schwinger)



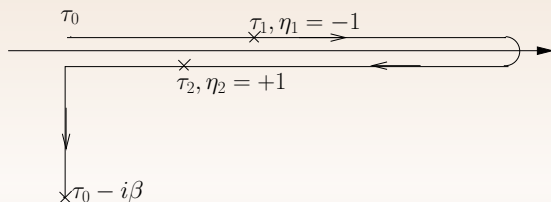
$$G(\tau_1\eta_1, \tau_2\eta_2) \Rightarrow \underline{G}(\tau_1, \tau_2) \Rightarrow \begin{pmatrix} G^R(\tau_1, \tau_2) & G^K(\tau_1, \tau_2) \\ 0 & G^A(\tau_1, \tau_2) \end{pmatrix}$$

After decay of transient: steady state $\underline{G}(\tau_1 - \tau_2) \Rightarrow \underline{G}(\omega)$

Needs dissipation, i.e. infinite system

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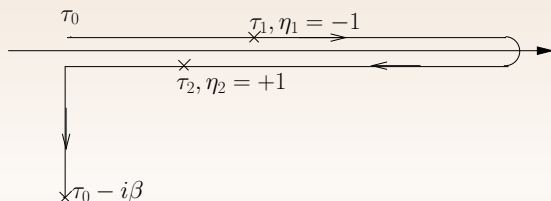
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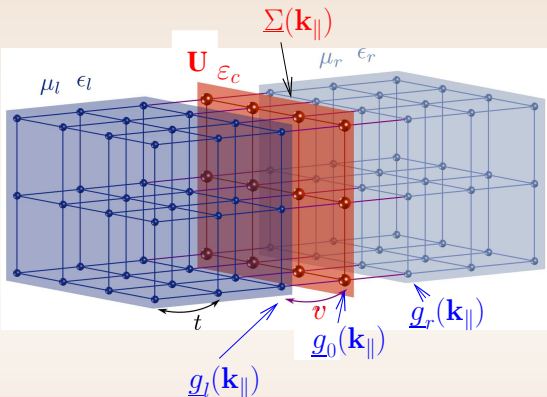


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Dynamical Mean-Field Theory



$v = 0$ Green's functions:

$$(g_0(\mathbf{k}_{\parallel})^{-1})^R = (\omega - \varepsilon_c - t(\mathbf{k}_{\parallel}))$$

$$(g_0(\mathbf{k}_{\parallel})^{-1})^K = 0$$

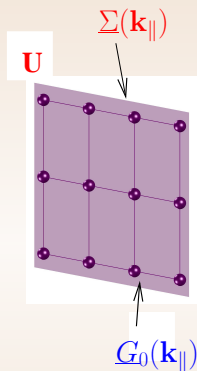
$$g_{\alpha}^R(\mathbf{k}_{\parallel}) = g_{\frac{1}{2}\text{chain}}^R(\omega - \varepsilon_{\alpha} - t(\mathbf{k}_{\parallel}))$$

$$g_{\alpha}^K(\mathbf{k}_{\parallel}) = 2i\text{Im} g_{\alpha}^R(\mathbf{k}_{\parallel})(1 - 2f_F(\omega - \mu_{\alpha}))$$

Dyson equation: (omit ω dependence)

$$\underline{G}(\mathbf{k}_{\parallel})^{-1} = \underline{g}_0^{-1}(\mathbf{k}_{\parallel}) - \sum_{\alpha=l,r} v^2 \underline{g}_{\alpha}(\mathbf{k}_{\parallel}) - \underline{\Sigma}(\mathbf{k}_{\parallel})$$

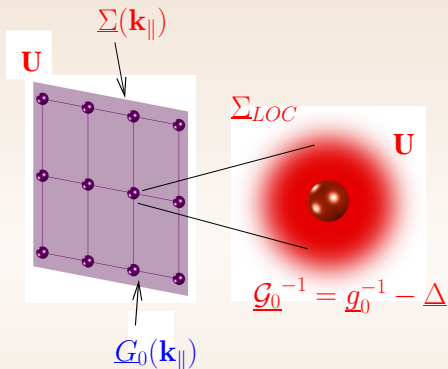
Dynamical Mean-Field Theory



noninteracting leads can be eliminated

$$\underline{G}(\mathbf{k}_{\parallel})^{-1} = \underline{G}_0(\mathbf{k}_{\parallel})^{-1} - \underline{\Sigma}(\mathbf{k}_{\parallel})$$

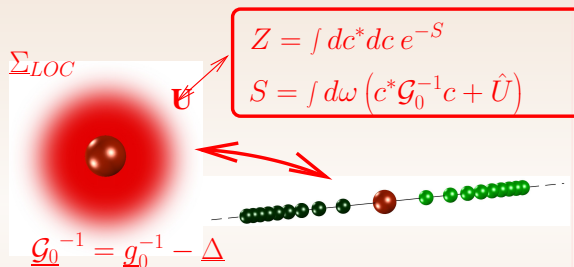
Dynamical Mean-Field Theory



DMFT approximates $\underline{\Sigma}(\mathbf{k}_{\parallel})$ by a local $\underline{\Sigma}_{LOC}$ obtained by solving an effective (nonequilibrium) **impurity** problem

$$\underline{G}_{IMP}^{-1} = \underline{g}_0^{-1} - \underline{\Sigma}_{LOC} = \underline{g}_0^{-1} - \underline{\Delta} - \underline{\Sigma}_{LOC}$$

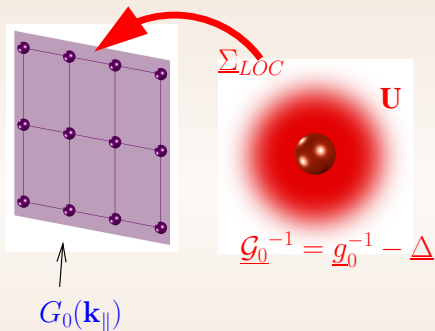
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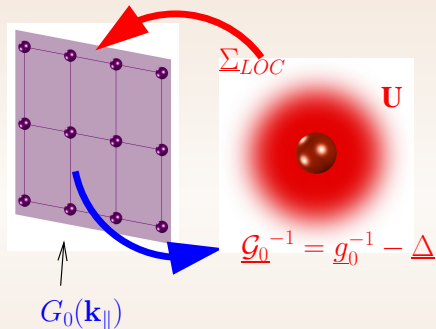
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Σ_{LOC} is used in the Dyson equation

$$\underline{G}(\mathbf{k}_{\parallel}) = (\underline{G}_0(\mathbf{k}_{\parallel})^{-1} - \underline{\Sigma}_{LOC})^{-1}$$

Dynamical Mean-Field Theory



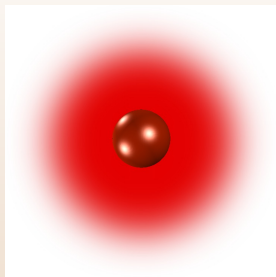
to obtain the self-consistent equation for **bath hybridisation function** $\underline{\Delta}$

$$\int_{BZ} \frac{d\mathbf{k}_{\parallel}}{(2\pi)^2} \underline{G}(\mathbf{k}_{\parallel}) \equiv \underline{G}_{LOC} = \underline{G}_{IMP} \equiv \left(\underline{g}_0^{-1} - \underline{\Delta} - \underline{\Sigma}_{LOC} \right)^{-1}$$

DMFT Impurity solvers

Bottleneck

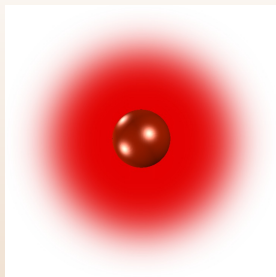
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is fitted by a small number of baths sites



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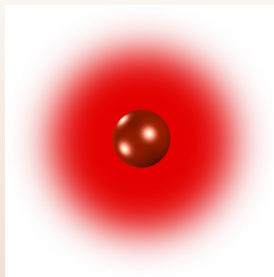
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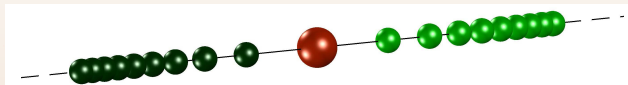
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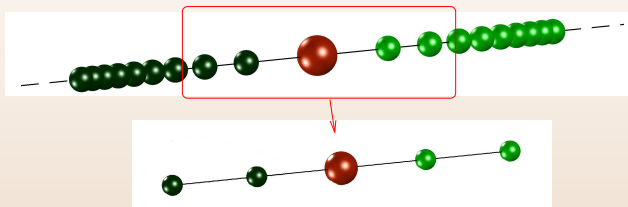
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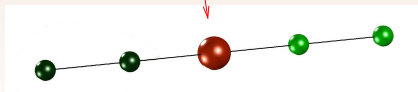
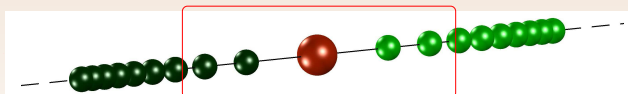
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Exact diagonalisation of a finite cluster

Does it work for a nonequilibrium steady-state?

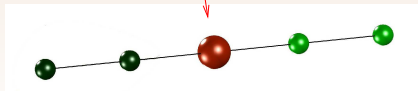
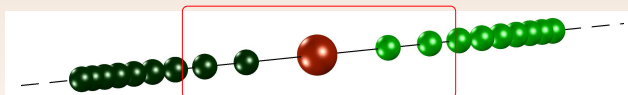


Problems in nonequilibrium:

- **Time dependence:** steady state is never reached (quasiperiodic behavior)
- Alternative: use equilibrium self energy:
at what chemical potential? Temperature?
- $\underline{\Delta}(\omega)$ must be fitted in **real frequency**
(Matsubara frequencies do not exist) **problem: peak structure**

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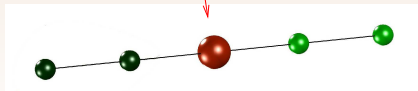
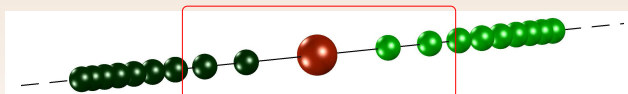


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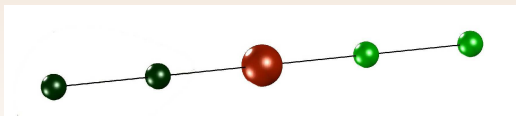
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Effective quantum Master equation approach



Dynamics described by Markovian Master equation for density matrix ρ of “chain” (Lindblad 76):

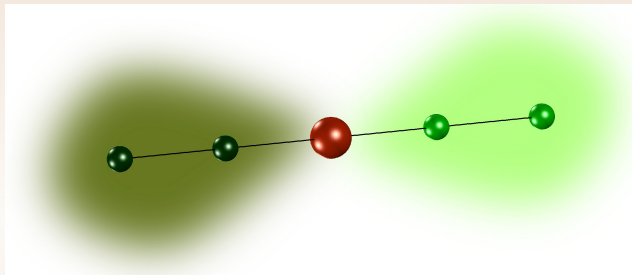
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Effective quantum Master equation approach

Attach two Markovian baths near the end of the chain:



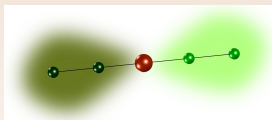
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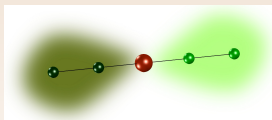
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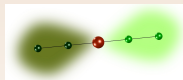
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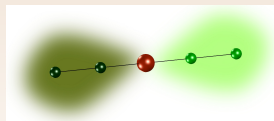
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Effective quantum Master equation approach



- Markovian Master equation: $\frac{d}{d\tau} \rho = \mathcal{L} \rho$
- Can be solved by exact diagonalisation: steady state, Green's function, and thus Σ_{LOC} can be determined
- Reproduces well the exact $\underline{\Delta}(\omega)$ already with a few number of chain sites.
- $U = 0$ Green's function does not have "delta-peak" structure. Can be used to fit $\underline{\Delta}(\omega)$ for real ω .
- Markovian baths exactly describe a system with infinite bandwidth and $\mu = \pm\infty$.
However, both are reduced effectively at the impurity site due to the chain sites in between.

Solution of the many-body Master equation

by exact diagonalisation (see e.g. Schmutz 78)

- Mapping onto a many-body problem with twice as many fermions

$$c_{r,\sigma} \Rightarrow \{c_{r,\sigma,A}, c_{r,\sigma,B}\}$$

“super” Hilbert space describe the space of density matrices

- Time dependence is controlled by the non-hermitian “superHamiltonian” $i\mathcal{L}$
- “Eigenvector” with zero eigenvalues is the steady-state density matrix ρ_{SS}
- Quantum regression theorem allows for evaluation of \underline{G}_{IMP} and thus $\underline{\Sigma}_{LOC}$

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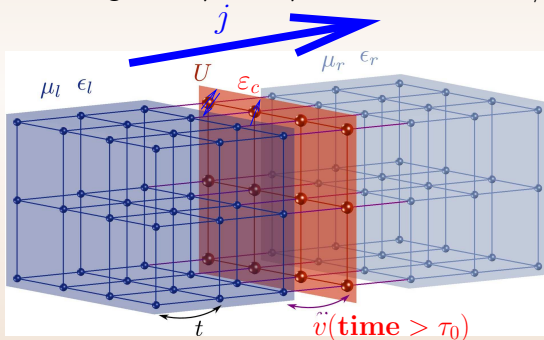
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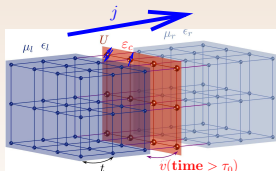
Model again

Parameters: Hopping $t = 1$, hopping to baths $v = \sqrt{0.1}$,
Voltage $\phi = \mu_l - \mu_r$.

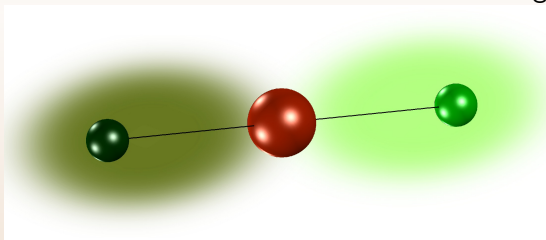
Half-filling: $\varepsilon_l = \mu_l = -\mu_r = -\varepsilon_r$, $\varepsilon_c = -U/2$.



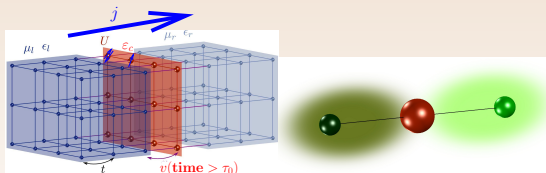
Fit of bath hybridisation function $\underline{\Delta}(\omega)$



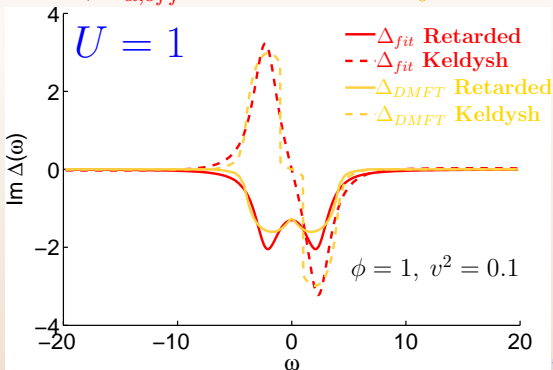
Fit of $\text{Im } \Delta^R$ and $\text{Im } \Delta^K$ with three chain sites \Rightarrow 8 fitting parameters.

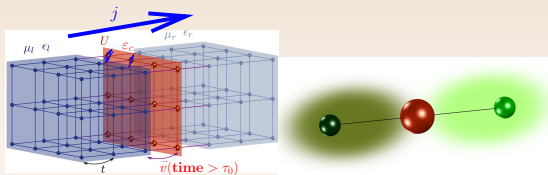


$$\Delta_{\text{fit}} = v^2 \sum_{\alpha=l,r} g_{\alpha,\text{eff}} \quad \text{vs.} \quad \Delta_{\text{DMFT}} = g_0^2 - G_{l,0}^2 - \sum_{\alpha} \dots$$

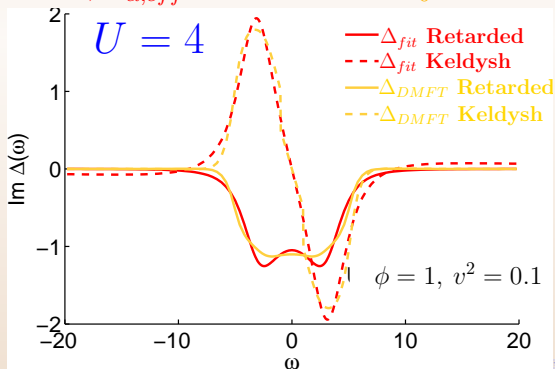
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$$\underline{\Delta}_{fit} = v^2 \sum_{\alpha=l,r} \underline{g}_{\alpha,eff} \quad \text{vs.} \quad \underline{\Delta}_{DMFT} = \underline{g}_0^{-1} - \underline{G}_{LOC}^{-1} - \underline{\Sigma}_{LOC}$$



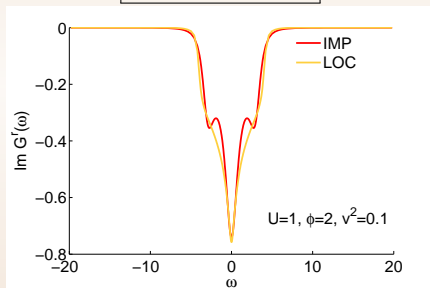
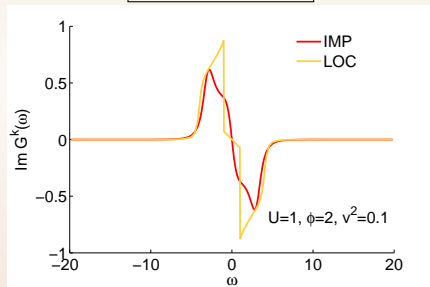
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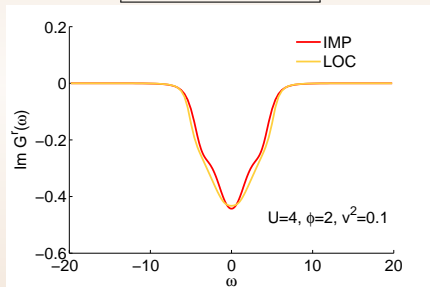
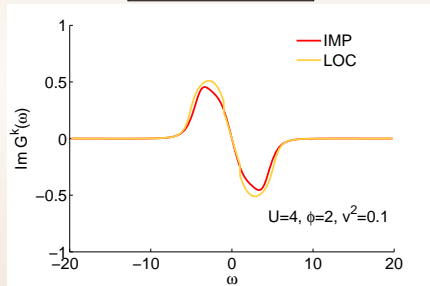
Local Green's function

$$U = 1, \text{ Voltage } \phi = 2$$

 $\text{Im } G^{\text{Retarded}}$

 $\text{Im } G^{\text{Keldysh}}$


Local Green's function

$$U = 4, \text{ Voltage } \phi = 2$$

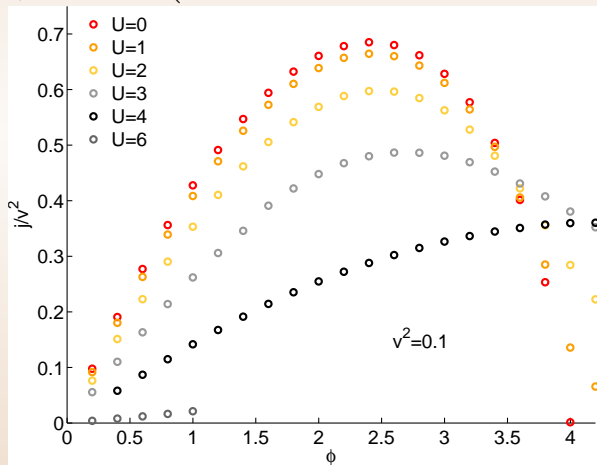
 $\text{Im } G^{\text{Retarded}}$

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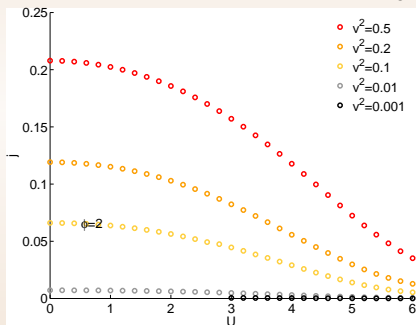
Current vs voltage ϕ

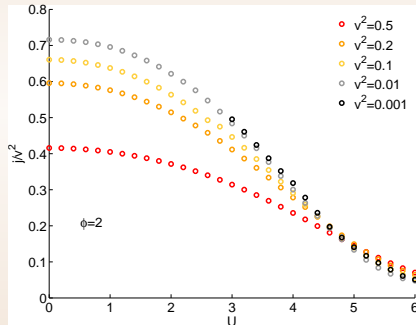
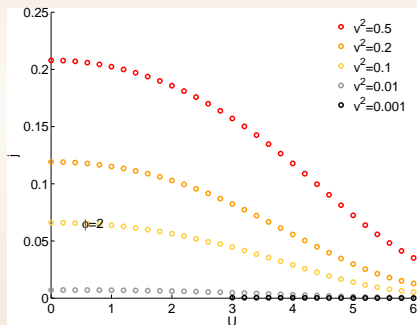
at different U

Current density

$$J \propto v \int_{BZ} \frac{d\mathbf{k}_{\parallel}}{(2\pi)^2} \int d\omega \operatorname{Re} \left(G_{layer}^R(\omega, \mathbf{k}_{\parallel}) g_l^K(\omega, \mathbf{k}_{\parallel}) + G_{layer}^K(\omega, \mathbf{k}_{\parallel}) g_l^A(\omega, \mathbf{k}_{\parallel}) \right)$$



Current vs. U at different v Voltage $\phi = 2$ 

Current vs. U at different v Voltage $\phi = 2$ 

1 Introduction

2 Model and Method

- Nonequilibrium DMFT
- Impurity solver by an effective quantum Master equation approach

3 Results

4 Summary and Outlook

Thanks to



Michael Knap

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Michael Knap



Wolfgang von der Linden

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also:

Martin Nuss

(Nonequilibrium VCA)

E. Arrighoni et al. (ITP^{CP} / TU Graz)

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Wolfgang von der Linden

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Project P24081-N16



Summary and Outlook

- Approach to solve the DMFT impurity problem based on Exact diagonalisation of an effective Lindblad quantum Master equation
- Problem: “Super”-Hilbert space is much larger
However: Number of fit parameters also increases faster.

Outlook:

- Time dependence:
 - Floquet theory (Floquet-DMFT)
 - Floquet-DMFT (Bloch oscillations)
 - Floquet treatment
- Cluster extensions: variational cluster approach, cluster dynamical mean-field theory
- Solutions with DMRG or quantum trajectory approaches

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