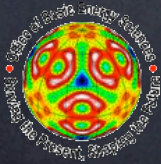




Evora, 11/2008

Spin Liquid States in Frustrated Antiferromagnets

Leon Balents
KITP



The David and Lucile Packard Foundation

Evora, 11/2008

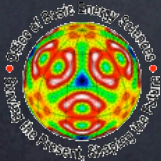


Looking
for

Spin Liquid States in Frustrated Antiferromagnets

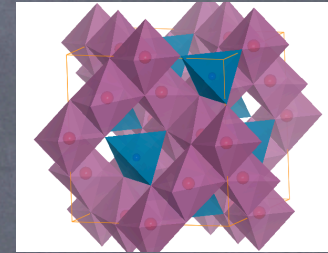
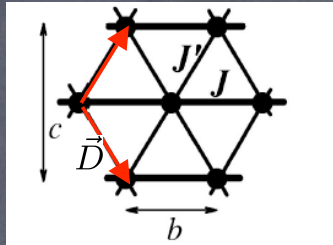
and finding
surprises

Leon Balents
KITP



The David and Lucile Packard Foundation

Collaborators



• Oleg Starykh, U. Utah



• Gang Chen, UCSB



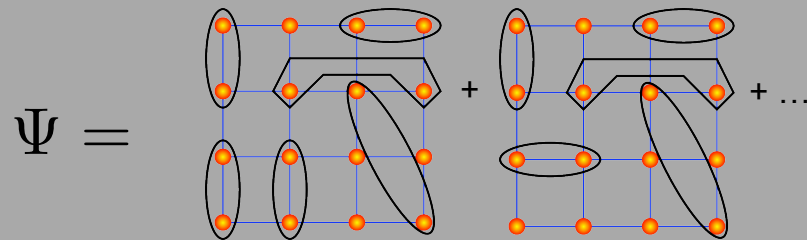
• Masanori Kohno, NIMS, Japan



• Andreas Schnyder, KITP

Quantum Spin Liquids

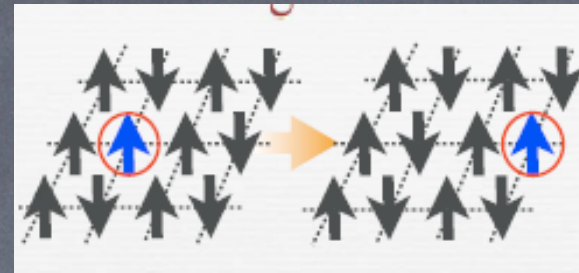
- QSL: a state of a magnet in which quantum fluctuations prevent order even at $T=0$.
- Many theoretical suggestions since Anderson (73)
 - “Resonating Valence Bond” QSL states



Magnons

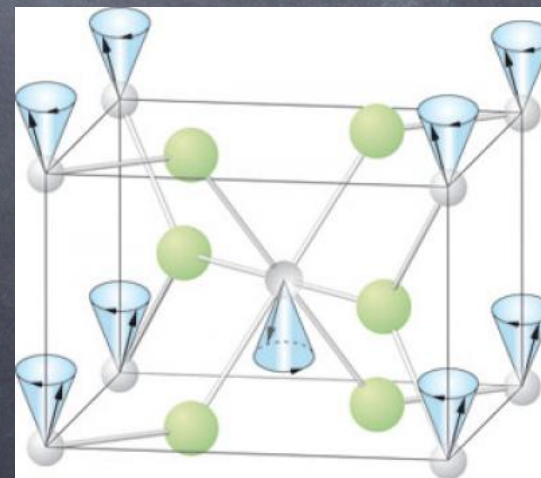
- Basic excitation: spin flip

 - Carries " S^z " = ± 1



- Periodic Bloch states: spin waves

 - Quasi-classical picture: small precession



MnF_2



$$\epsilon = \hbar\omega(\vec{k})$$

Image: B. Keimer

One dimension

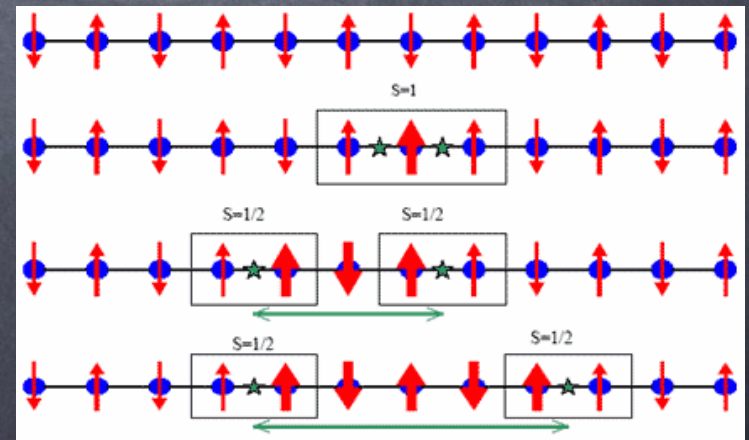
- Heisenberg model is a *spin liquid*

- No magnetic order $\langle \vec{S}(x) \cdot \vec{S}(x') \rangle \sim \frac{(-1)^{x-x'}}{|x-x'|} + \dots$

- Power law correlations of spins and dimers

- Excitations are $s=1/2$ *spinons*

- General for 1d chains



Spinons by neutrons

- Bethe ansatz:

- Spinon energy

- Spin-1 states

$$\epsilon_s(k) = \frac{\pi J}{2} |\sin k|$$

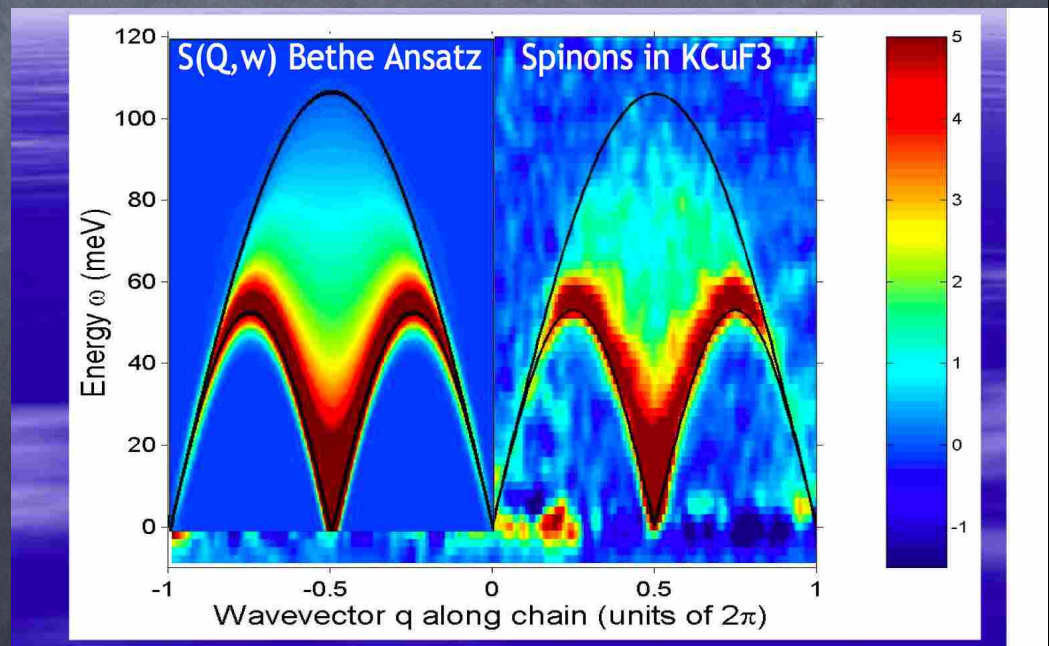
$$k = k_1 + k_2$$

$$\epsilon = \epsilon_s(k_1) + \epsilon_s(k_2)$$

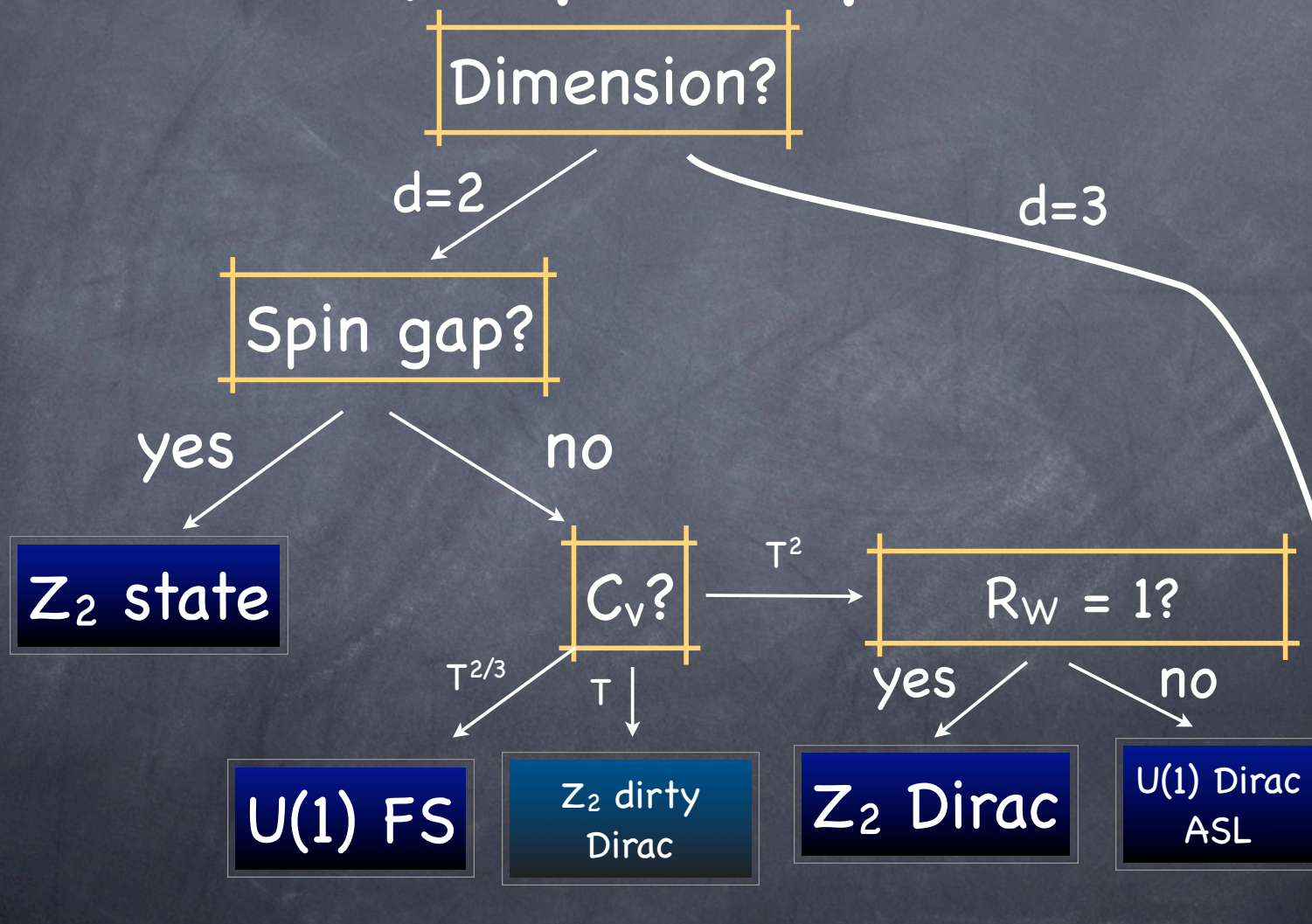
} 2-particle
continuum

- Theory vs experiment
for KCuF_3 with
anisotropy ≈ 30

- B. Lake, HMI

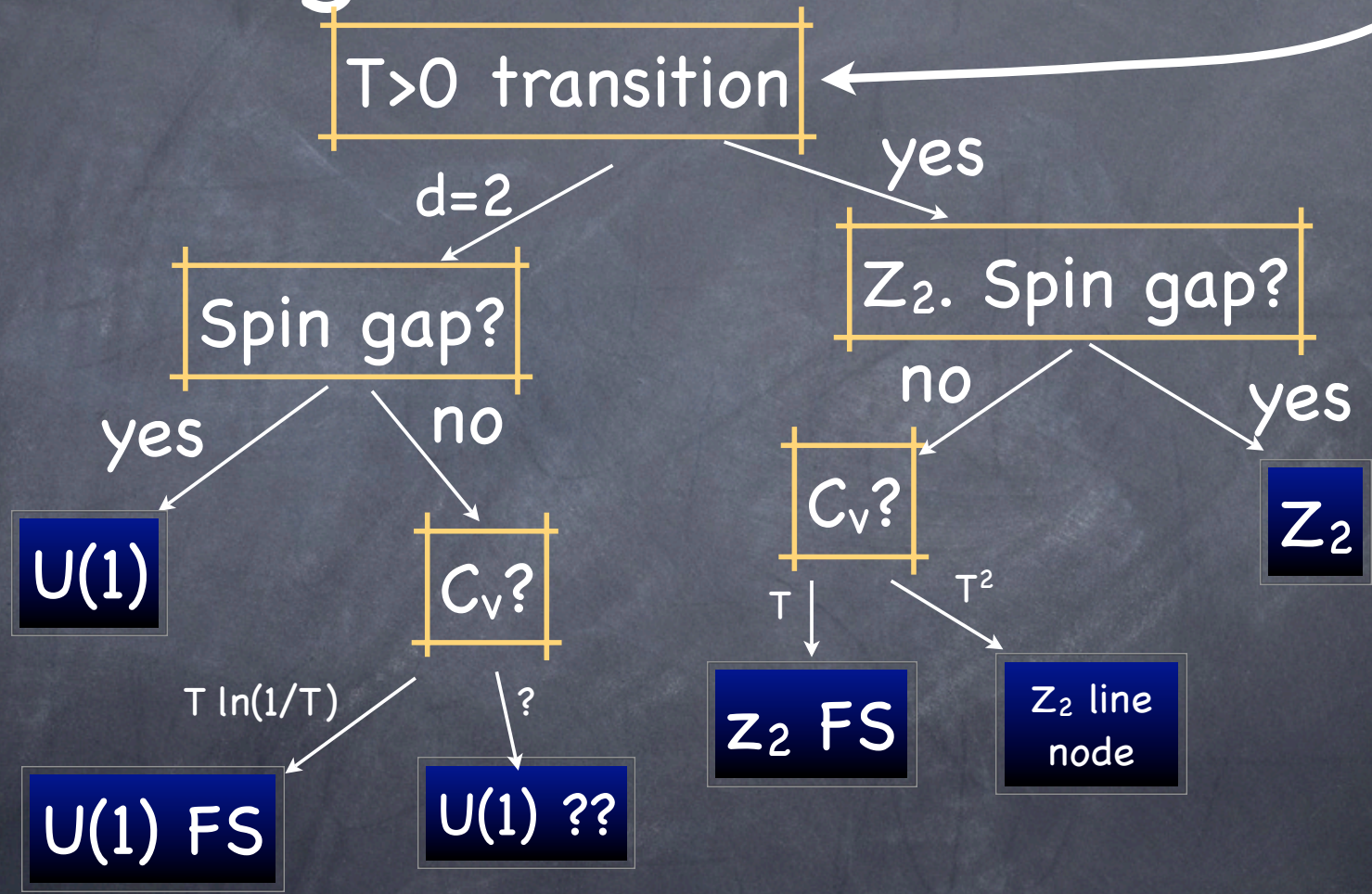


Many spin liquids in theory!



d=3

A diagnostic flowchart



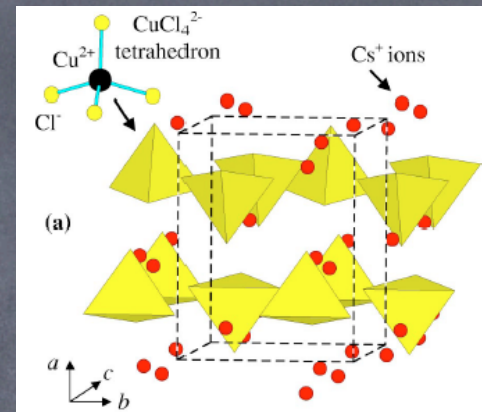
disordered possibilities neglected

QSL candidates

- ● CsCu_2Cl_4 - spin-1/2 anisotropic triangular lattice
- ? ● NiGa_2S_4 - spin-1 triangular lattice
- $\kappa\text{-(BEDT-TTF)}_2\text{Cu}_2(\text{CN})_3$, $\text{EtMe}_3\text{Sb}[\text{Pd}(\text{dmit})_2]_2$ - triangular lattice organics
- ● FeSc_2S_4 - orbitally degenerate spinel
- ? ● $\text{Na}_4\text{Ir}_3\text{O}_8$ - hyperkagome
- $\text{ZnCu}_3(\text{OH})_6\text{Cl}_2$ - kagome

Cs_2CuCl_4

- Spatially anisotropic triangular lattice
- Cu^{2+} spin-1/2 spins



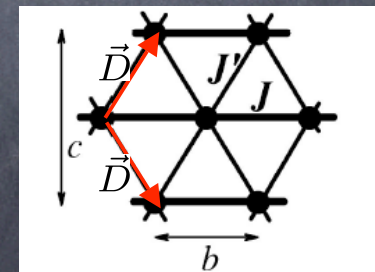
$$H = \frac{1}{2} \sum_{ij} \left[J_{ij} \vec{S}_i \cdot \vec{S}_j - \vec{D}_{ij} \cdot \vec{S}_i \times \vec{S}_j \right]$$

- couplings:

$$J = 0.37 \text{ meV}$$

$$J' = 0.3J$$

$$D = 0.05J$$

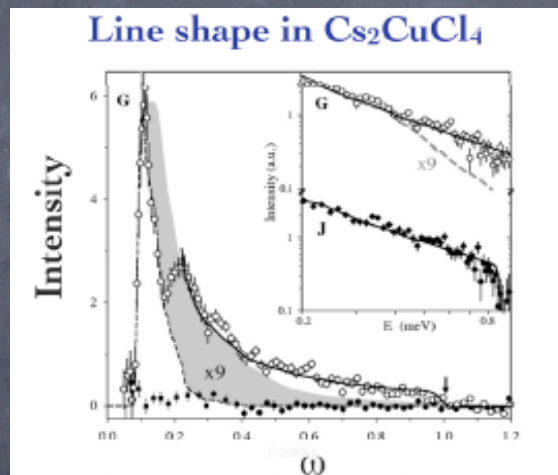


$$\vec{D} = D \hat{a}$$

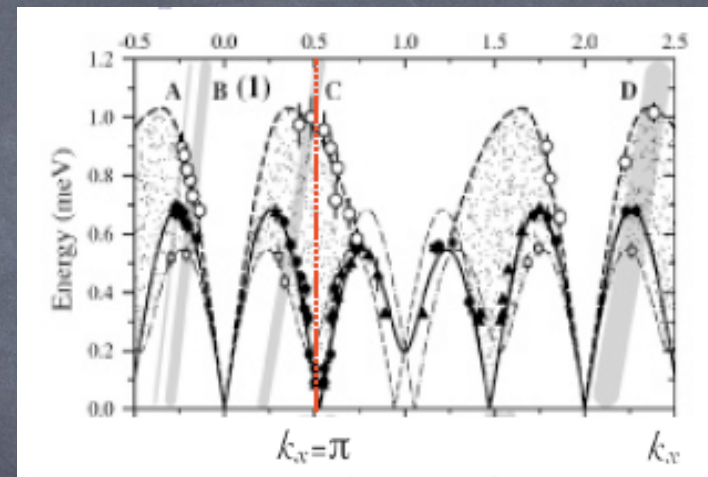
R. Coldea et al

Neutron scattering

- Coldea et al, 2001/03: a 2d spin liquid?



Very broad spectrum similar to 1d (in some directions of k space). Roughly fits power law.

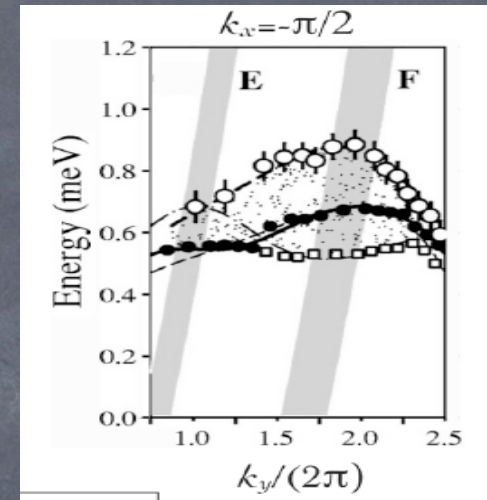


Fit of "peak" dispersion to spin wave theory requires adjustment of J, J' by 40% - in opposite directions!

2d theories

- Arguments for 2d:
 - $J'/J = 0.3$ *not very small*
 - Transverse dispersion
- Exotic theories:

- J.Alicea, O.I.Motrunich & M.P.Fisher:
Phys. Rev. Lett. **95**, 247203 (2005).
- S.V.Isakov, T.Senthil & Y.B.Kim:
Phys. Rev. B **72**, 174417 (2005).
- Y.Zhou & X.-G.Wen:
cond-mat/0210662.
- F.Wang & A.Vishwanath:
Phys. Rev. B **74**, 174423 (2006).
- C.-H.Chung, K.Voelker & Y. B. Kim:
Phys. Rev. B **68**, 094412 (2003).

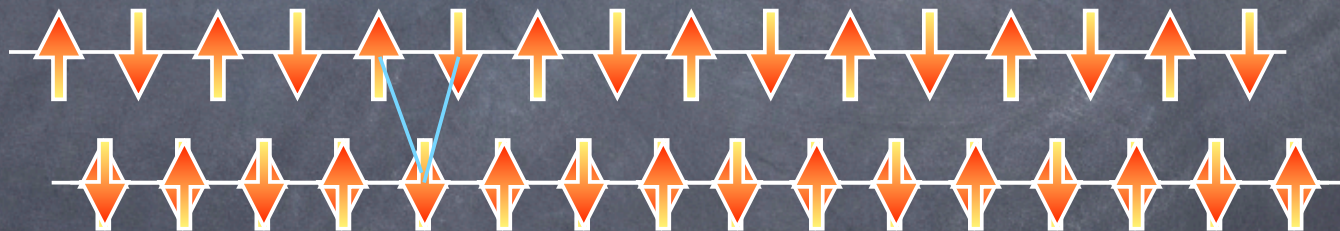


• Spin waves

- M.Y.Veillette, A.J.A.James & F.H.L.Essler:
Phys. Rev. B **72**, 134429 (2005).
- D.Dalidovich, R.Sknepnek, A.J.Berlinsky,
J.Zhang & C.Kallin:
Phys. Rev. B **73**, 184403 (2006).
- R.Coldea, D.A.Tennant & Z.Tylczynski:
Phys. Rev. B **68**, 134424 (2003).

Dimensional reduction?

- Frustration of interchain coupling makes it less "relevant"
 - First order energy correction vanishes

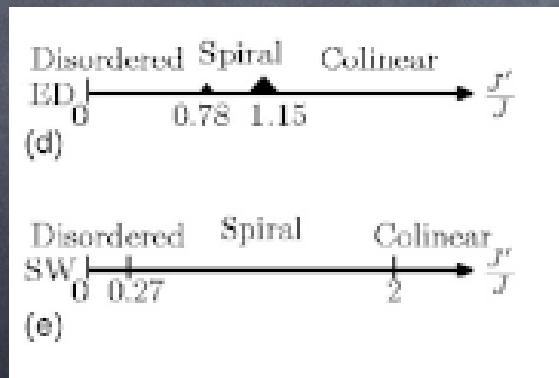


- Leading effects on correlations are in fact $O[(J')^4/J^3]$!

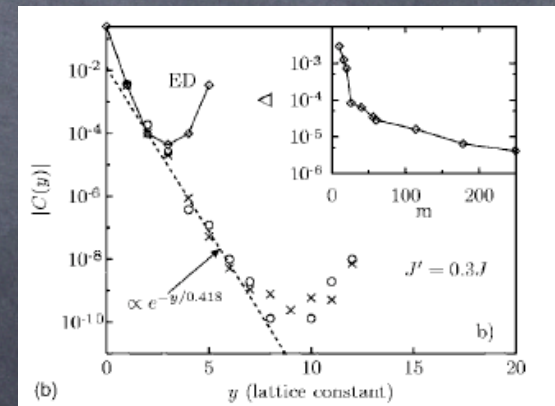
Dimensional reduction?

- Frustration of interchain coupling makes it less "relevant"
 - First order energy correction vanishes.
 - Numerics: $J'/J < 0.7$ is "weak"

Weng et al,
2006



Very different from
spin wave theory

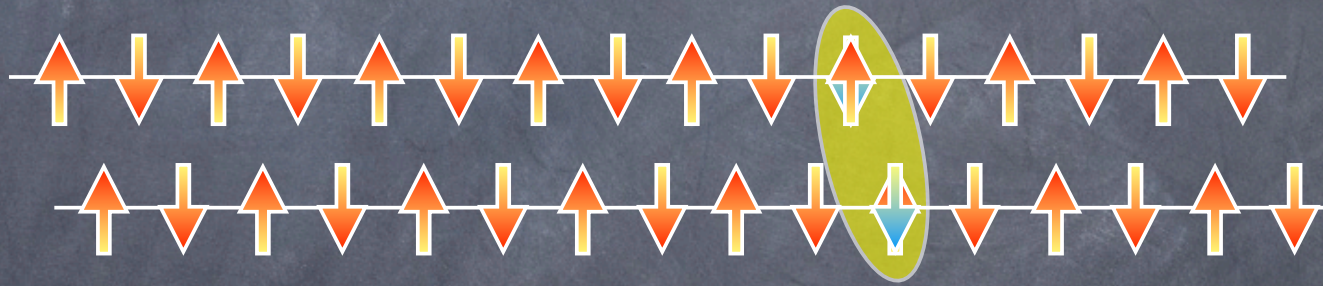


Very weak inter-chain
correlations

Excitations

- Build 2d excitations from 1d spinons

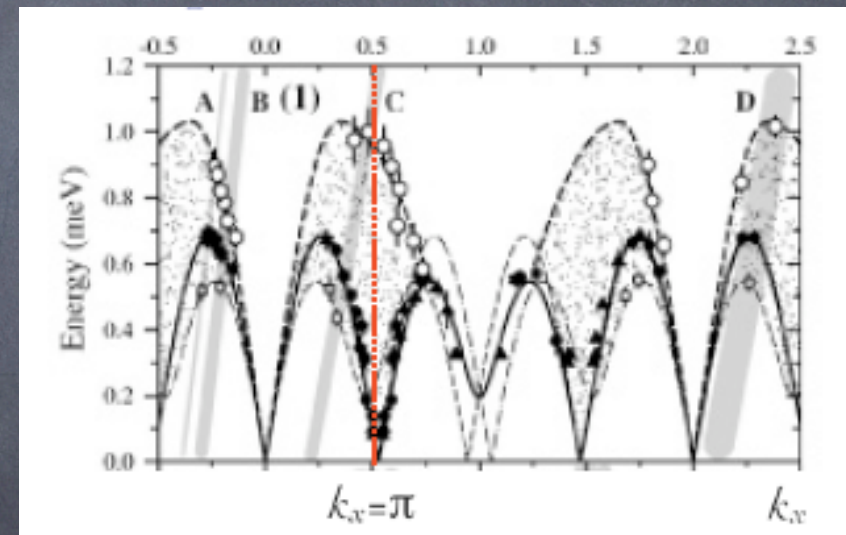
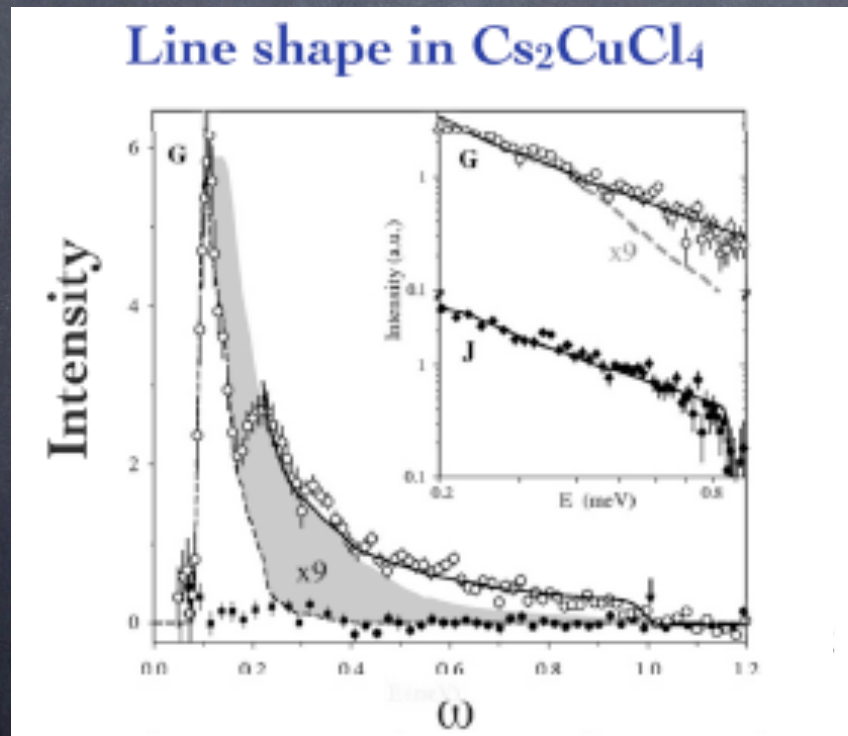
- Exchange:
$$\frac{J'}{2} (S_i^+ S_j^- + S_i^- S_j^+)$$



- Expect spinon binding to lower inter-chain kinetic energy
- Use 2-spinon Schroedinger equation

Broad lineshape: "free spinons"

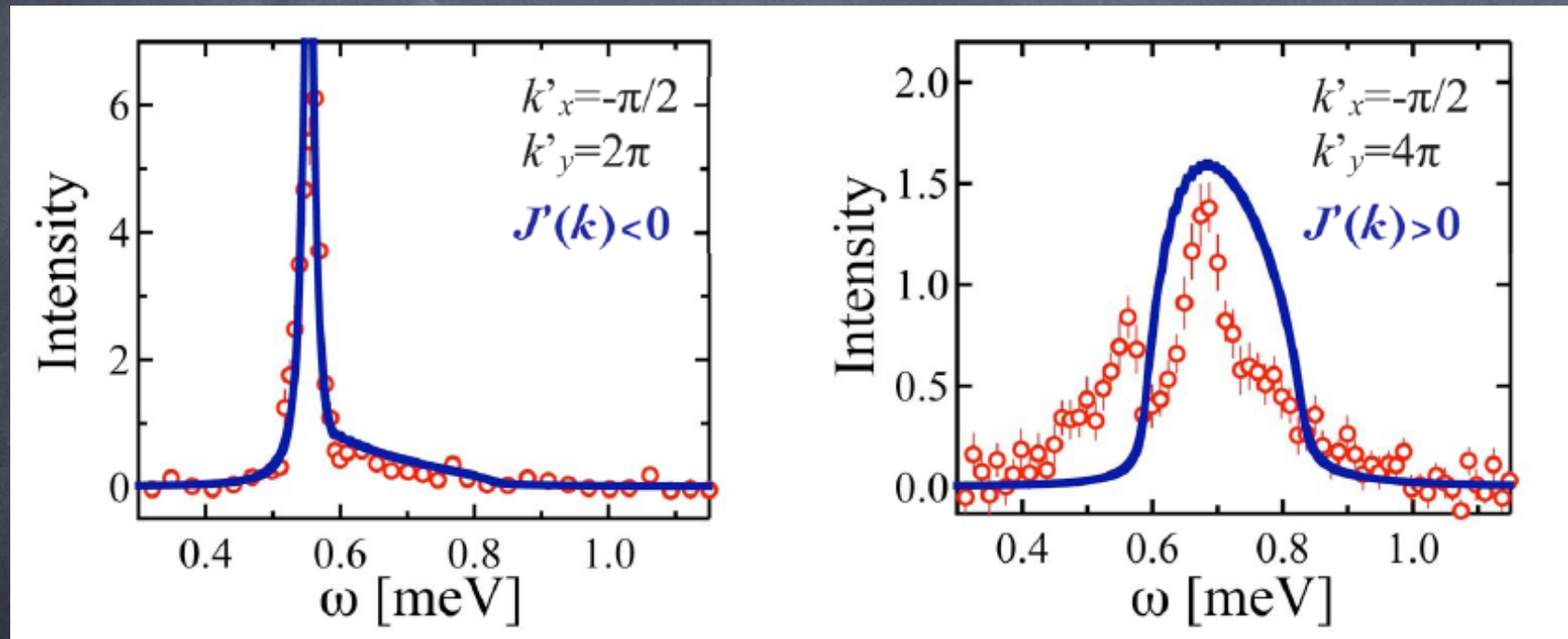
- "Power law" fits well to free spinon result
- Fit determines normalization



$J'(k)=0$ here

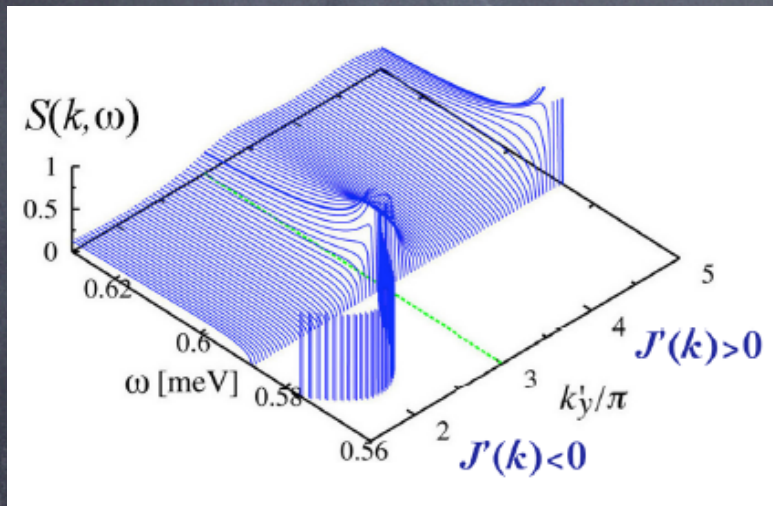
Bound state

- Compare spectra at $J'(k) < 0$ and $J'(k) > 0$:

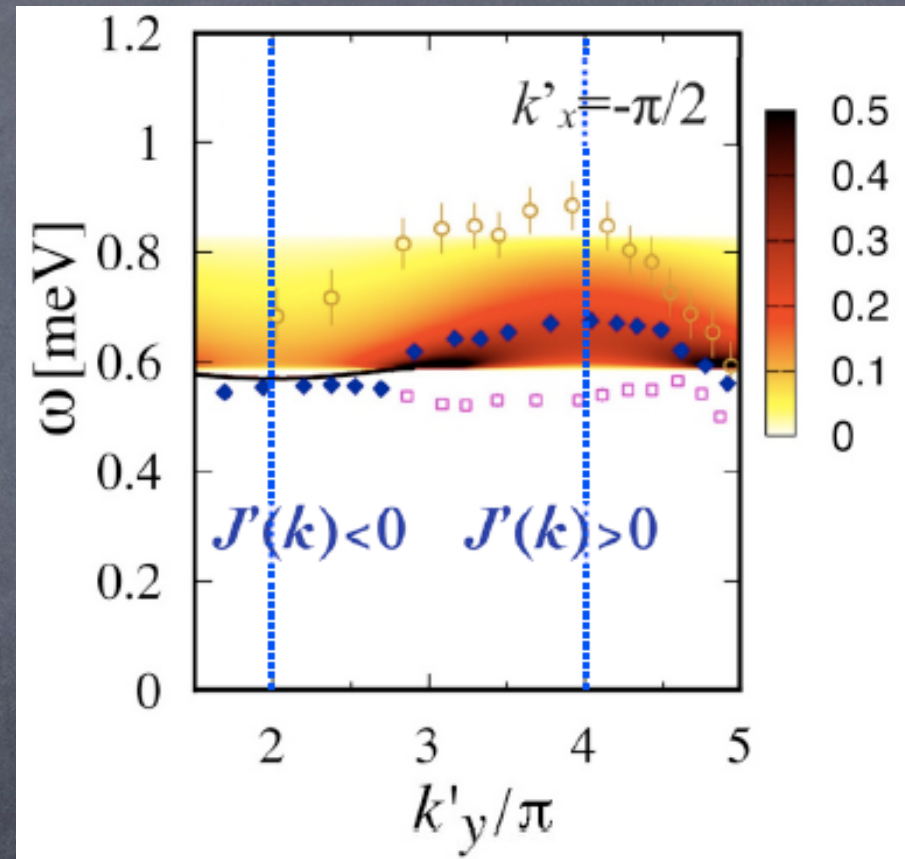


- [arXiv:1405.2433](https://arxiv.org/abs/1405.2433) / www.nature.com/articles/nature13287 / experimental resolution

Transverse dispersion

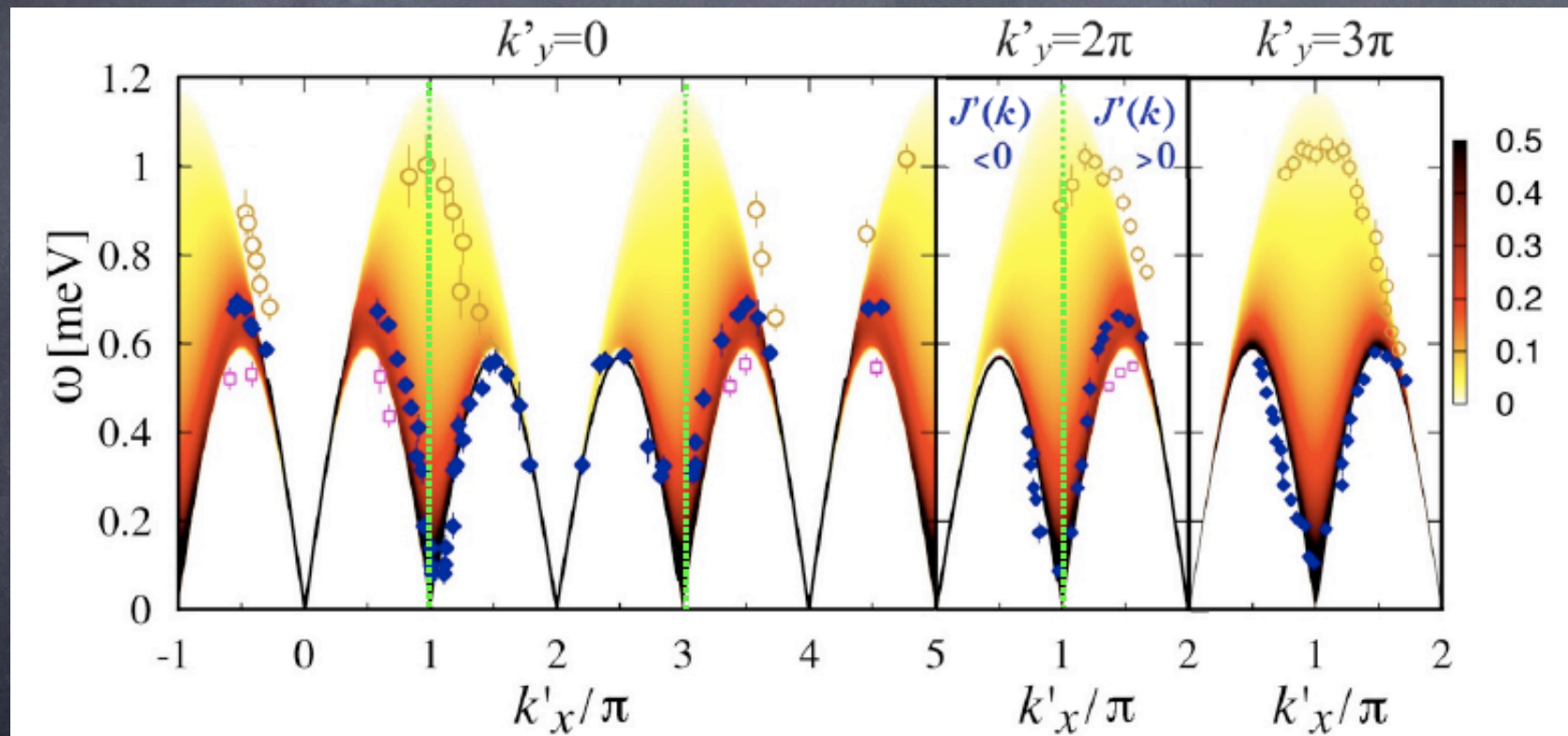


Bound state and resonance



Solid symbols: experiment
Note peak (blue diamonds) coincides with bottom edge only for $J'(k) < 0$

Spectral asymmetry



Vertical lines: $J'(k) = 0$.

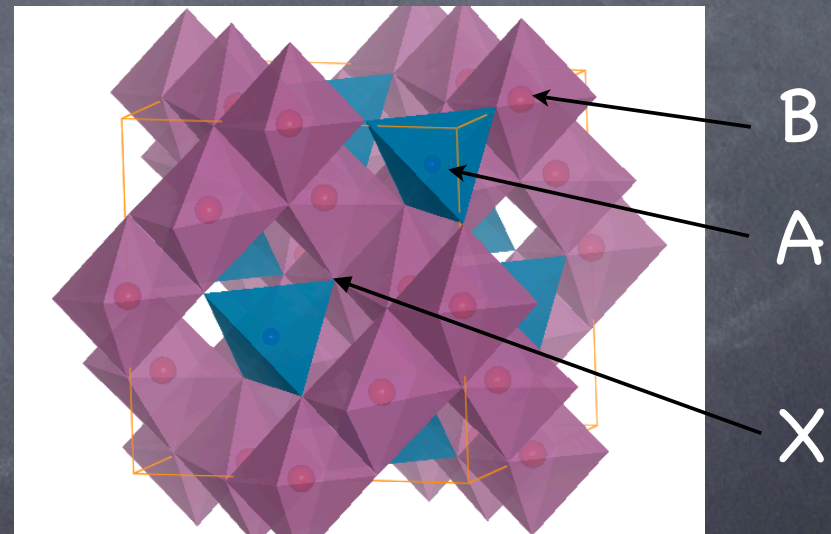
Conclusions on Cs_2CuCl_4

- Simple theory works well for frustrated quasi-1d antiferromagnets
 - Frustration leads to a strong enhancement of one-dimensionality
- The mystery of Cs_2CuCl_4 should be considered solved
 - Many (nearly all) other details of diverse experiments on this material may be understood in the same framework

AB_2X_4 spinels

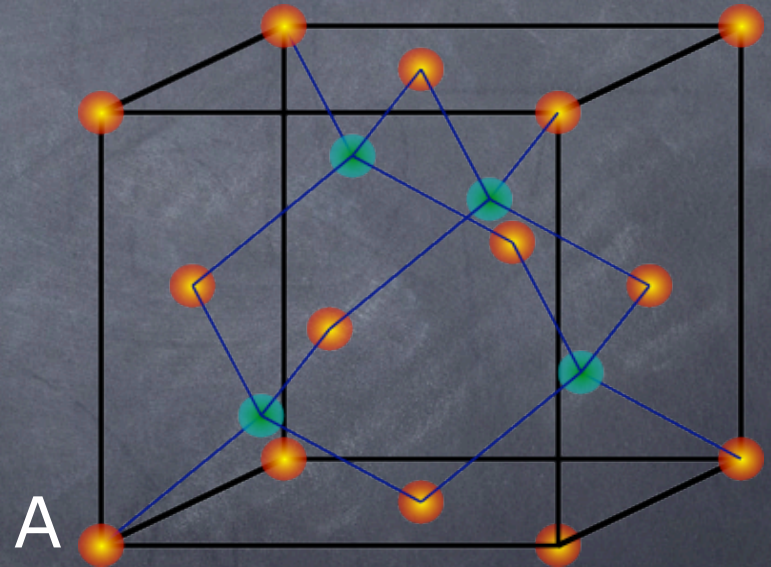
cubic $Fd\bar{3}m$

- One of the most common mineral structures
- Common valence:
 - A^{2+}, B^{3+}, X^{2-}
 - $X=O, S, Se$

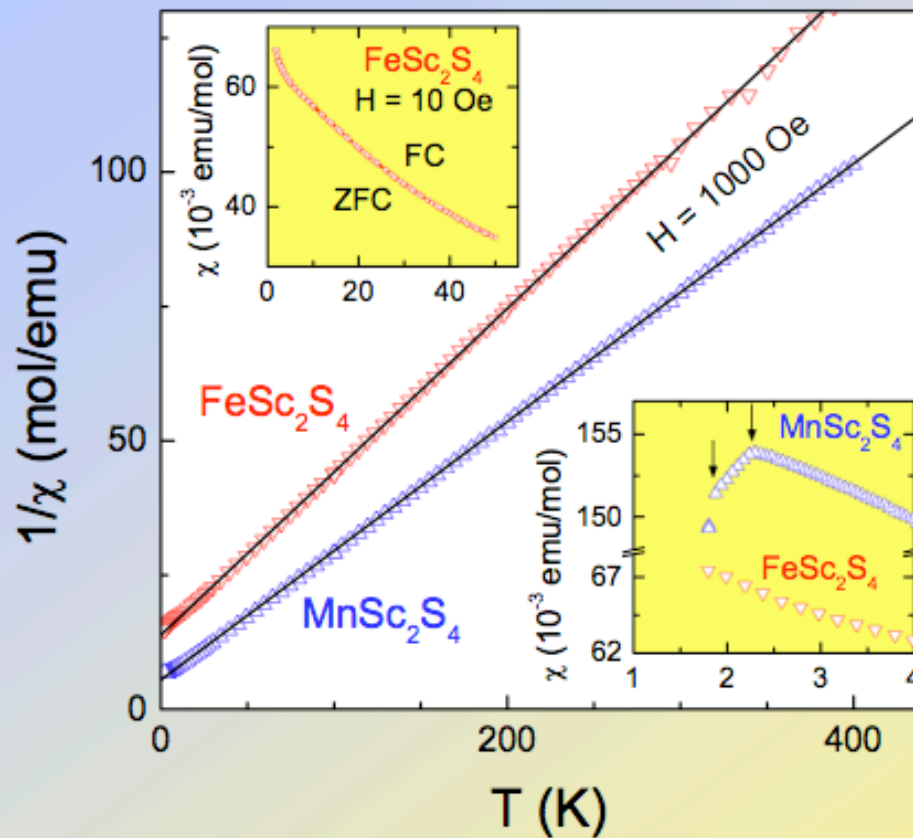


Deconstructing the spinel

- A atoms: diamond lattice
- Bipartite: not *geometrically* frustrated



Frustration Signature



FeSc₂S₄: $\theta_{CW} = 50$ K

T > 30 mK:

no long-range magnetic order

no spin-glass

MnSc₂S₄: $\theta_{CW} = 25$ K

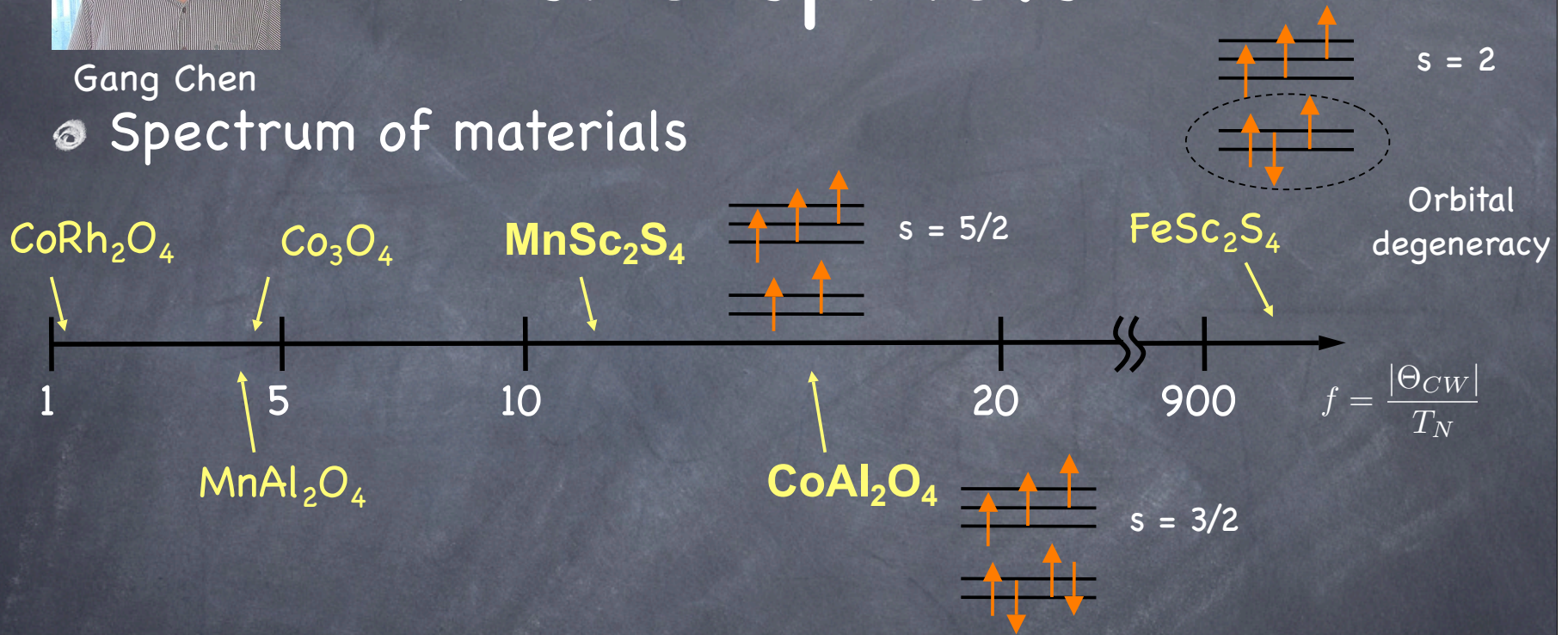
AFM transition @ 2 K



Gang Chen

Spectrum of materials

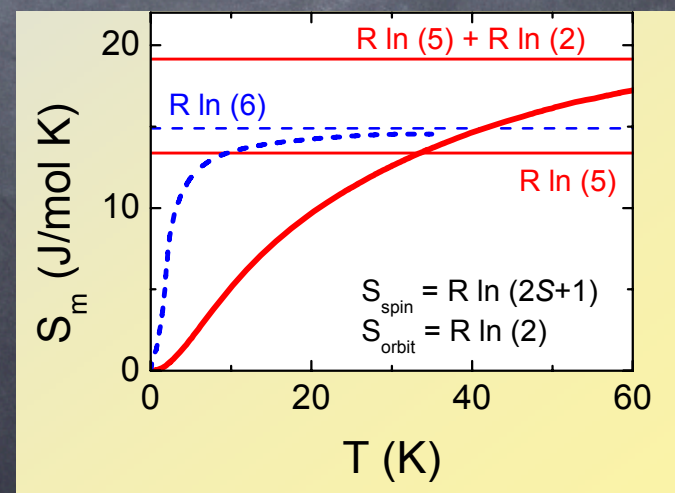
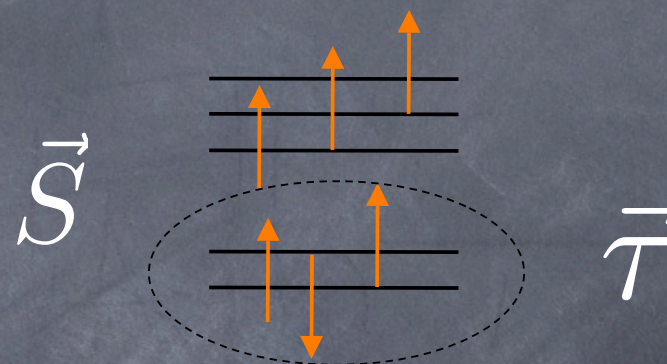
A-site spinels



V. Fritsch et al. PRL **92**, 116401 (2004); N. Tristan et al. PRB **72**, 174404 (2005); T. Suzuki et al. (2006)

Orbital degeneracy in FeSc_2S_4

- Chemistry:
 - Fe^{2+} : $3d^6$
 - 1 hole in e_g level
- Spin $S=2$
- Orbital pseudospin $1/2$
- Static Jahn-Teller does not appear



Atomic Spin Orbit

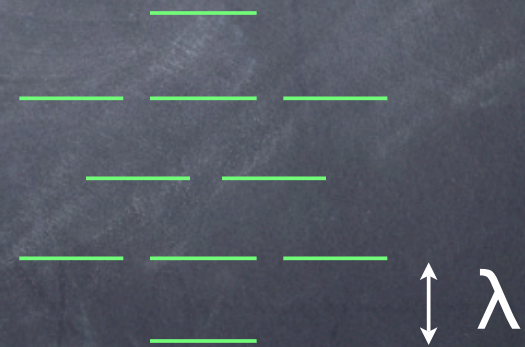
- Separate orbital and spin degeneracy can be split!

$$H_{SO} = -\lambda \left(\frac{1}{\sqrt{3}} \tau^x [(S^x)^2 - (S^y)^2] + \tau^z \left[(S^z)^2 - \frac{S(S+1)}{3} \right] \right)$$

- Energy spectrum: singlet GS with gap = λ

- Microscopically,

$$\lambda = \frac{6\lambda_0^2}{\Delta}$$



- Naive estimate $\lambda \approx 25\text{K}$

- should be reduced by dynamic JT

Spin orbital singlet

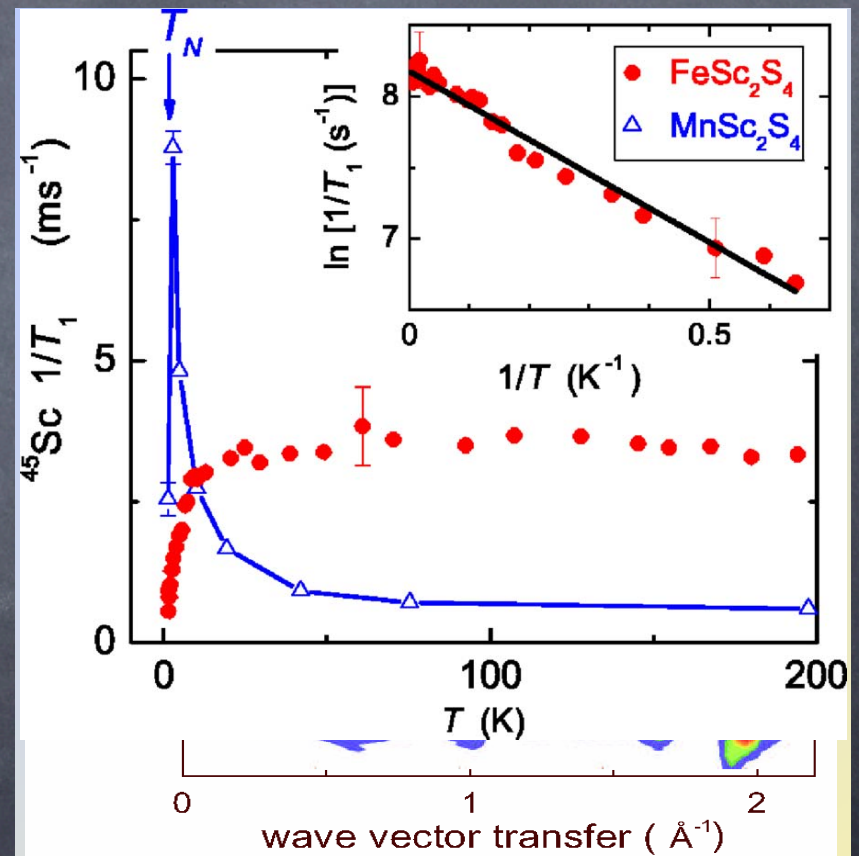
- Ground state of $\lambda > 0$ term:

$$\left| \begin{array}{c} \text{four-lobed orbital} \\ \text{with } S^z=0 \end{array} \right\rangle \left| S^z=0 \right\rangle - \frac{1}{\sqrt{2}} \left| \begin{array}{c} \text{two-lobed orbital} \\ \text{with } S^z=2 \text{ and } S^z=-2 \end{array} \right\rangle \left(\left| S^z=2 \right\rangle + \left| S^z=-2 \right\rangle \right)$$

- Due to gap, there is a stable SOS phase for $\lambda \gg J$.

Exchange

- Inelastic neutrons show significant dispersion indicating exchange
- Bandwidth $\approx 20\text{K}$ similar order as Θ_{CW} and estimated λ
- Gap (?) 1-2K
 - Small gap is classic indicator of incipient order



Exchange

- Most general symmetry-allowed form of exchange coupling (neglecting SOI)

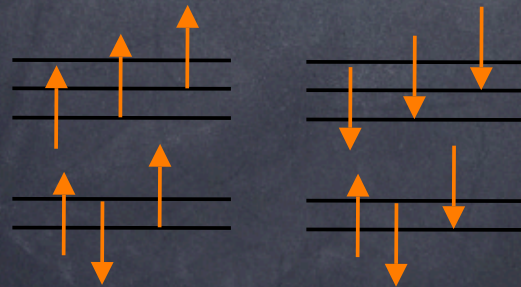
$$H_{ex} = \frac{1}{2} \sum_{ij} \left\{ J_{ij} \mathbf{S}_i \cdot \mathbf{S}_j + K_{ij} \boldsymbol{\tau}_i \cdot \boldsymbol{\tau}_j + \tilde{K}_{ij} \tau_i^y \tau_j^y \right. \\ \left. + \left[L_{ij} \boldsymbol{\tau}_i \cdot \boldsymbol{\tau}_j + \tilde{L}_{ij} \tau_i^y \tau_j^y \right] \mathbf{S}_i \cdot \mathbf{S}_j \right\}$$

Exchange

- Neglecting SOI, a simplified superexchange calculation gives

$$H_{ex} = \frac{1}{2} \sum_{ij} \{J_{ij} \mathbf{S}_i \cdot \mathbf{S}_j + K_{ij} (4 + \mathbf{S}_i \cdot \mathbf{S}_j) (1 + 4\boldsymbol{\tau}_i \cdot \boldsymbol{\tau}_j)\}$$

- Largest coupling is AF spin interaction $\mathbf{S}_i \cdot \mathbf{S}_j$
- More exchange processes

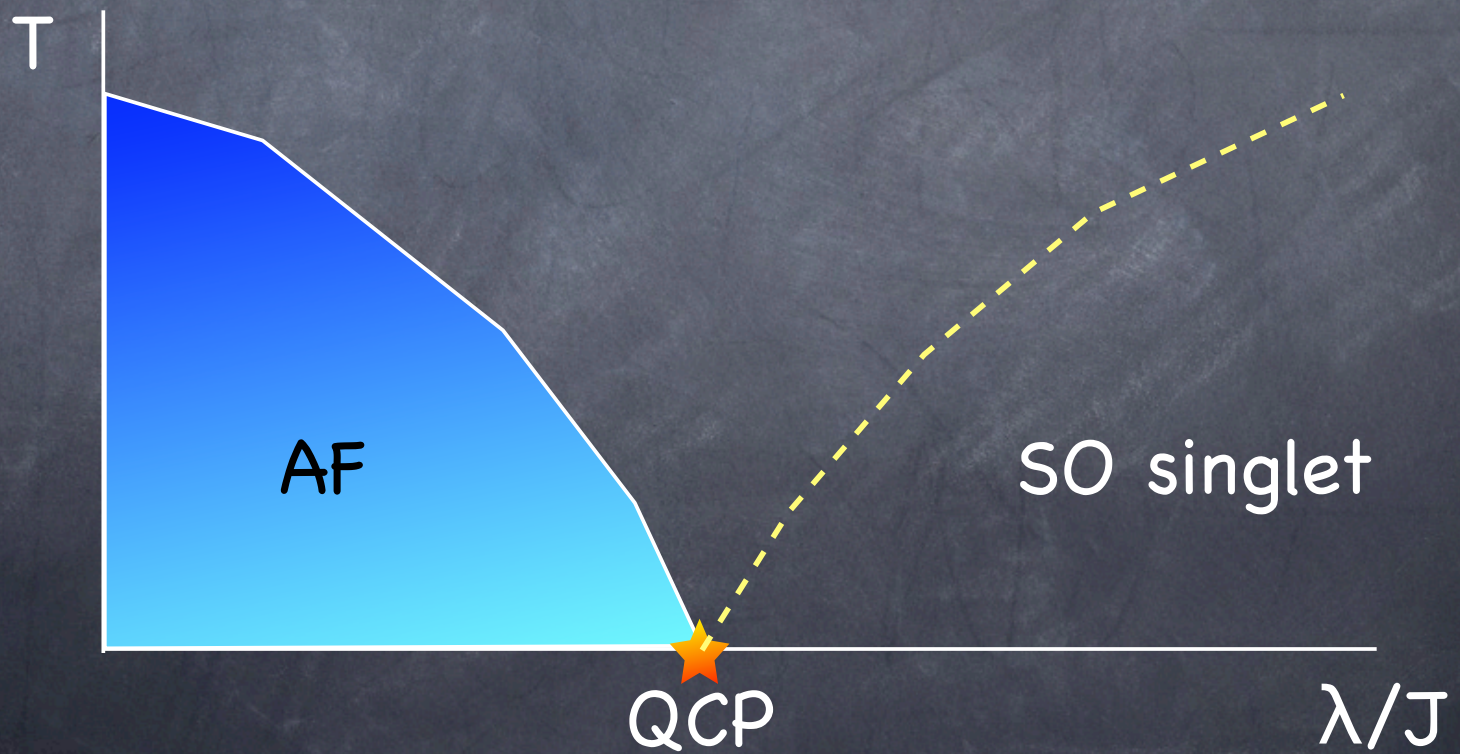


Ordered Phase ($J \gg \lambda$)

- Ground state of H_{ex} is almost certainly ordered
 - $S_i \cdot S_j$ coupling is strongest
 - Complex multi-spiral ground states possible
- Inclusion of weak SOI λ favors simpler commensurate "cubic" spin arrangements
 - spin order leads to induced orbital order

Quantum Critical Point

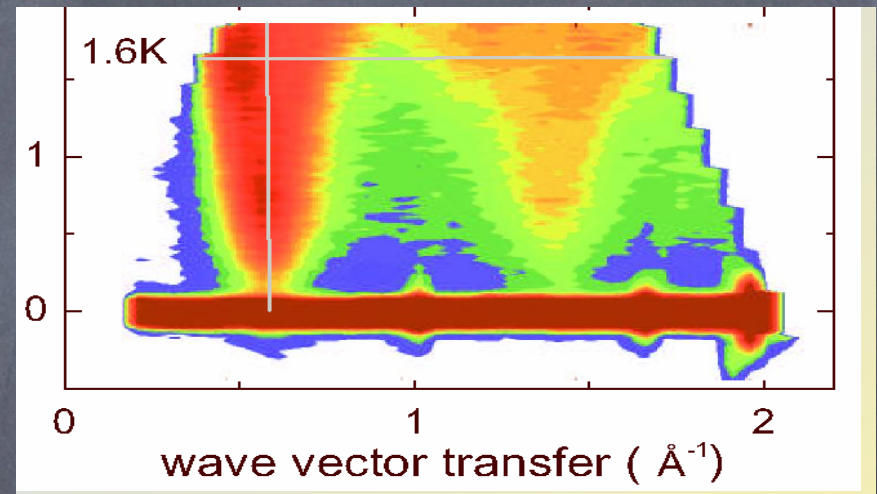
- Full Hamiltonian $H = H_{SO} + H_{ex}$



Minimal Model

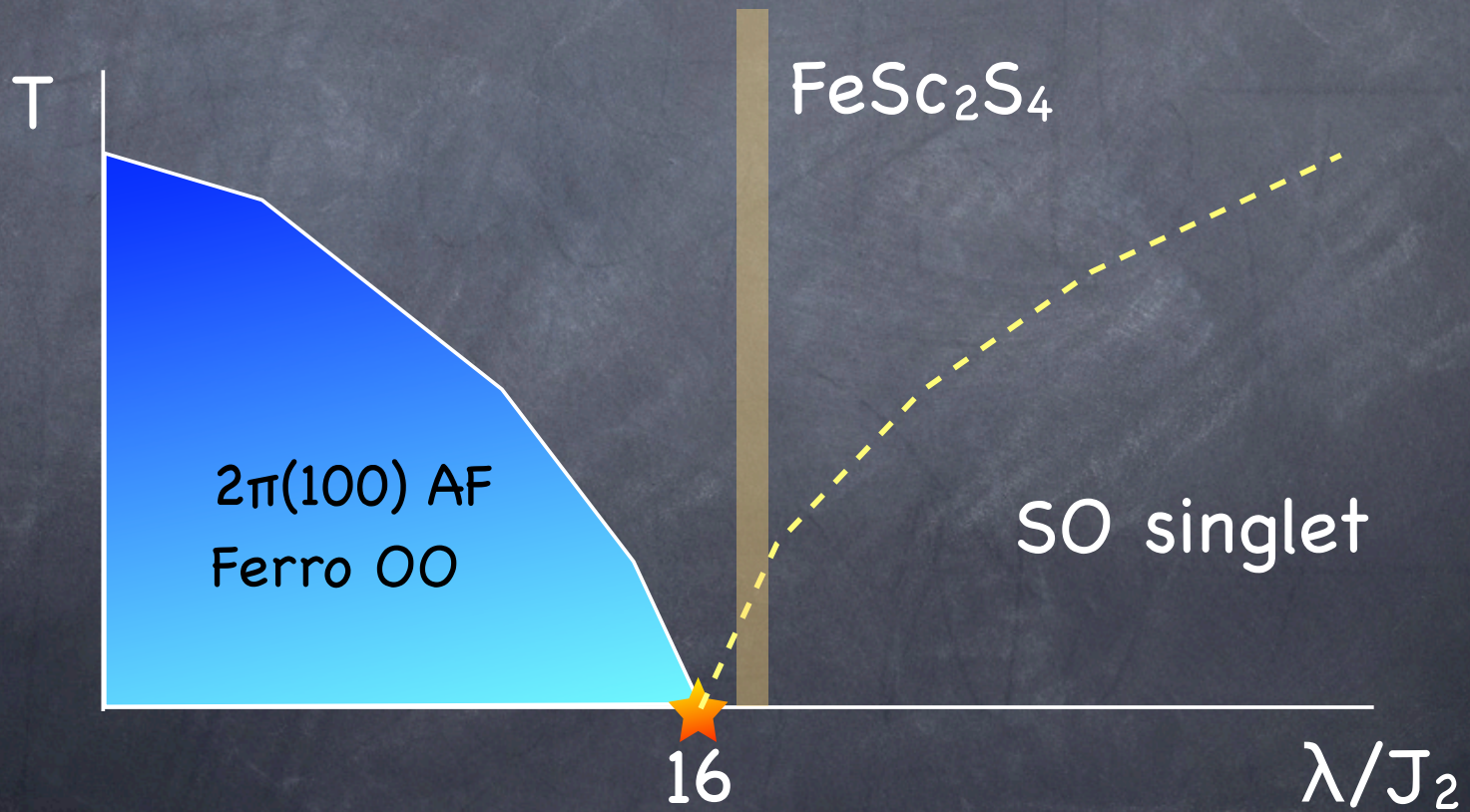
- Neutron scattering suggests peak close to $2\pi(100)$
- Indicates $J_2 \gg J_1$

$$H_{min} = J_2 \sum_{\langle\langle ij \rangle\rangle} \mathbf{S}_i \cdot \langle \mathbf{S}_j \rangle + H_{SO}$$



Quantum Critical Point

- Mean field phase diagram

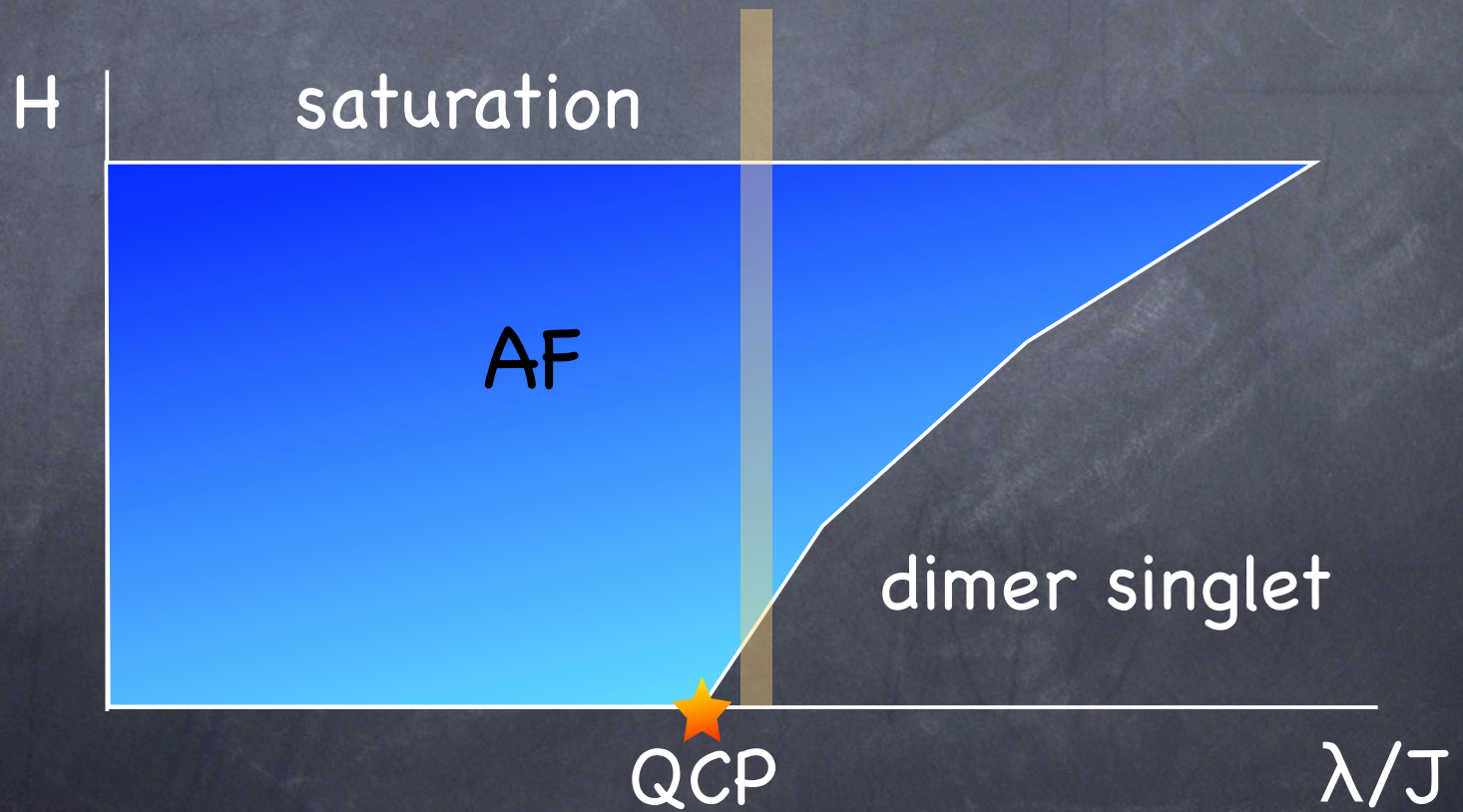


Consequences of QCP

- Power-law spin correlations
- Scaling form for $(T_1 T)^{-1} \sim f(\Delta/T)$
- Specific heat $C_v \sim T^3 f(\Delta/T)$
- Possibility of pressure-induced ordering
- Impurity effects?
- Behavior in field? Can triplet be made to condense?

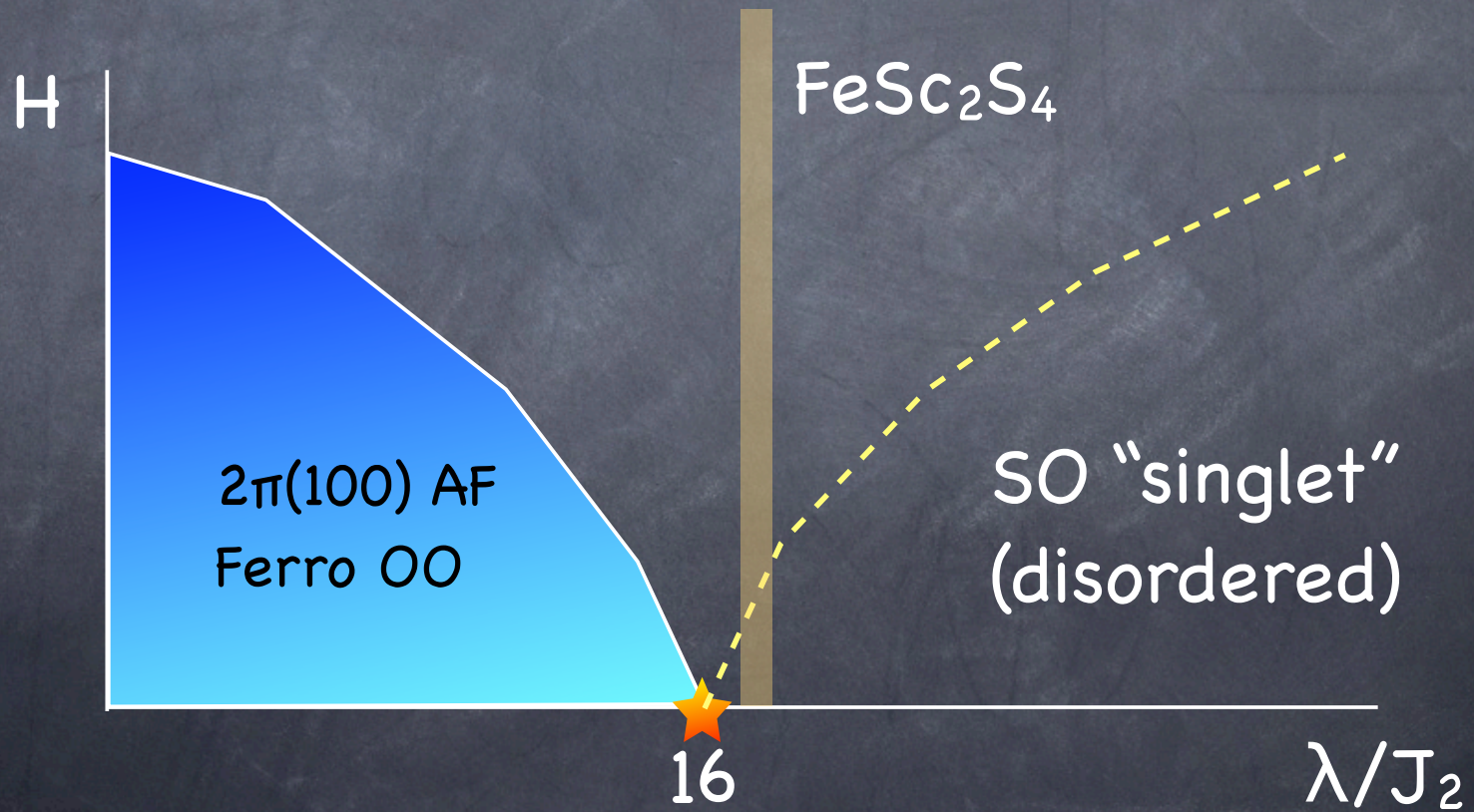
Behavior in Field

• c.f. dimer antiferromagnet



Behavior in field

⦿ This model



To Do List

- Effects of J_1 on QCP
 - transitions to incommensurate states?
- Phonons and Jahn-Teller effects
- More in-depth study of phases
 - Higher order expansion about $J=0$
 - Spin-wave corrections for ordered states
- Disorder and fields

Conclusions on FeSc_2S_4

- Orbital degeneracy and spin orbit provides an exciting route to quantum paramagnetism and quantum criticality
- entangled spin-orbital singlet ground state in an $S=2$ magnet!

More for the future!

- ✓ CsCu_2Cl_4 - spin-1/2 anisotropic triangular lattice
- ? NiGa_2S_4 - spin-1 triangular lattice
- $\kappa\text{-(BEDT-TTF)}_2\text{Cu}_2(\text{CN})_3$, $\text{EtMe}_3\text{Sb}[\text{Pd}(\text{dmit})_2]_2$ - triangular lattice organics
- ✓ FeSc_2S_4 - orbitally degenerate spinel
- ? $\text{Na}_4\text{Ir}_3\text{O}_8$ - hyperkagome
- $\text{ZnCu}_3(\text{OH})_6\text{Cl}_2$ - kagome