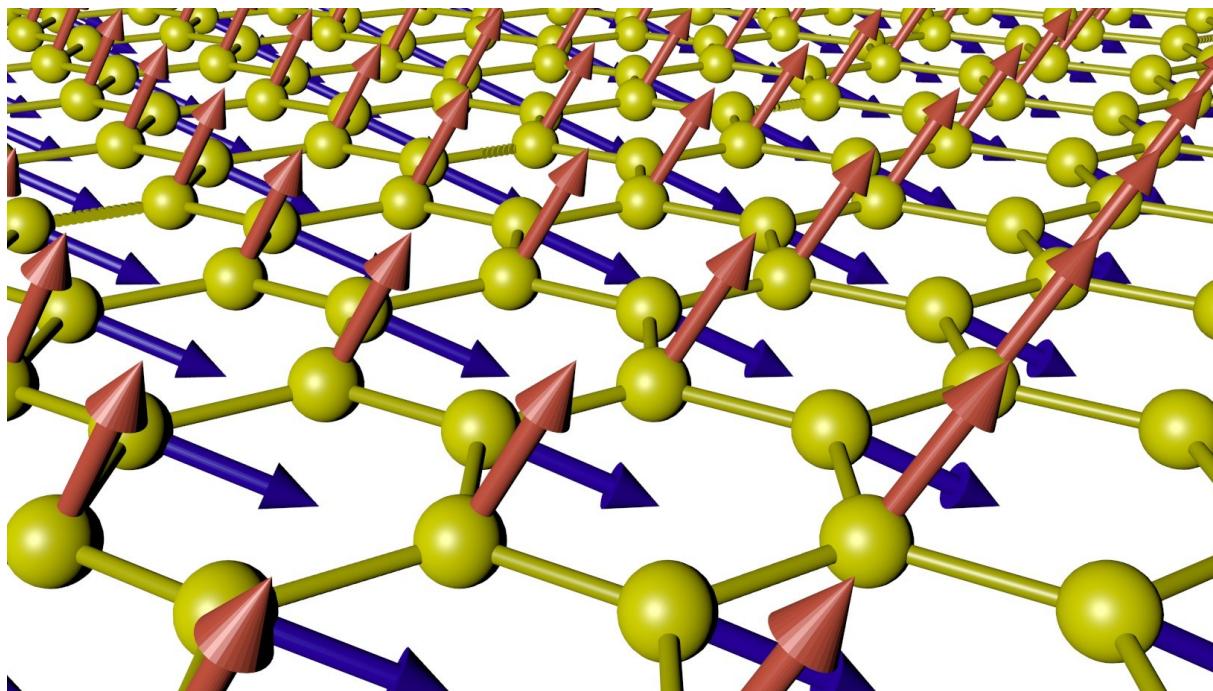


Magnetism and electronics in quantum Hall bars

Jose Lado and Joaquin Fernandez Rossier

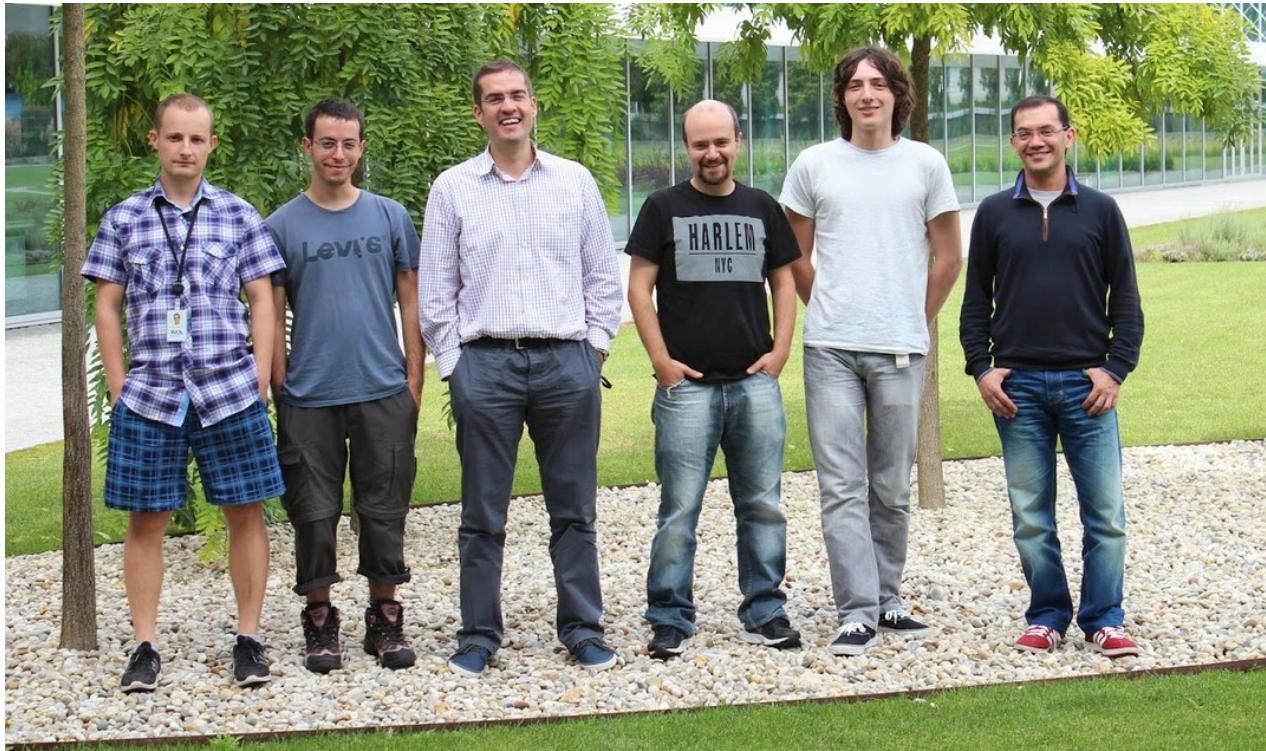
International Nanotechnology Laboratory (INL), Braga, Portugal



Evora 2014, 8 October

The team

Theory group at INL, Braga, Portugal

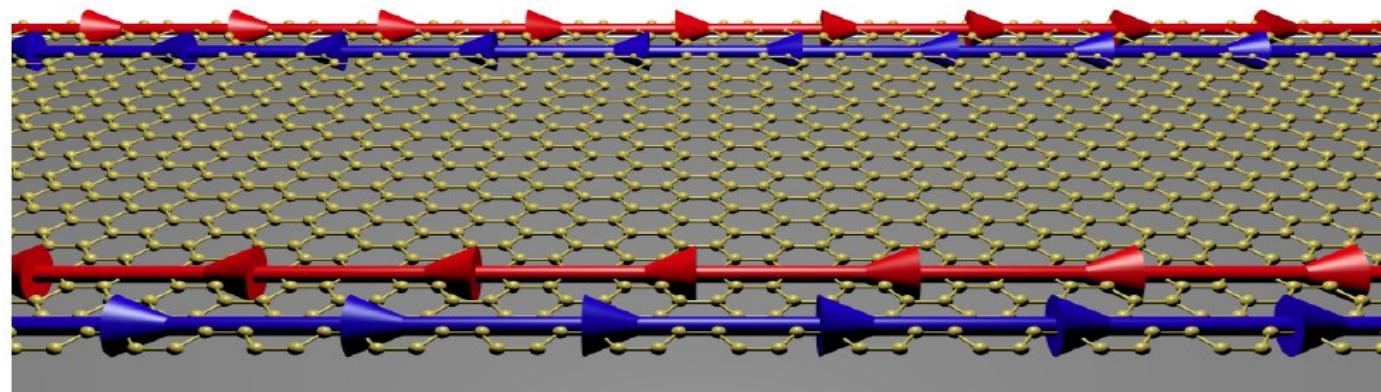
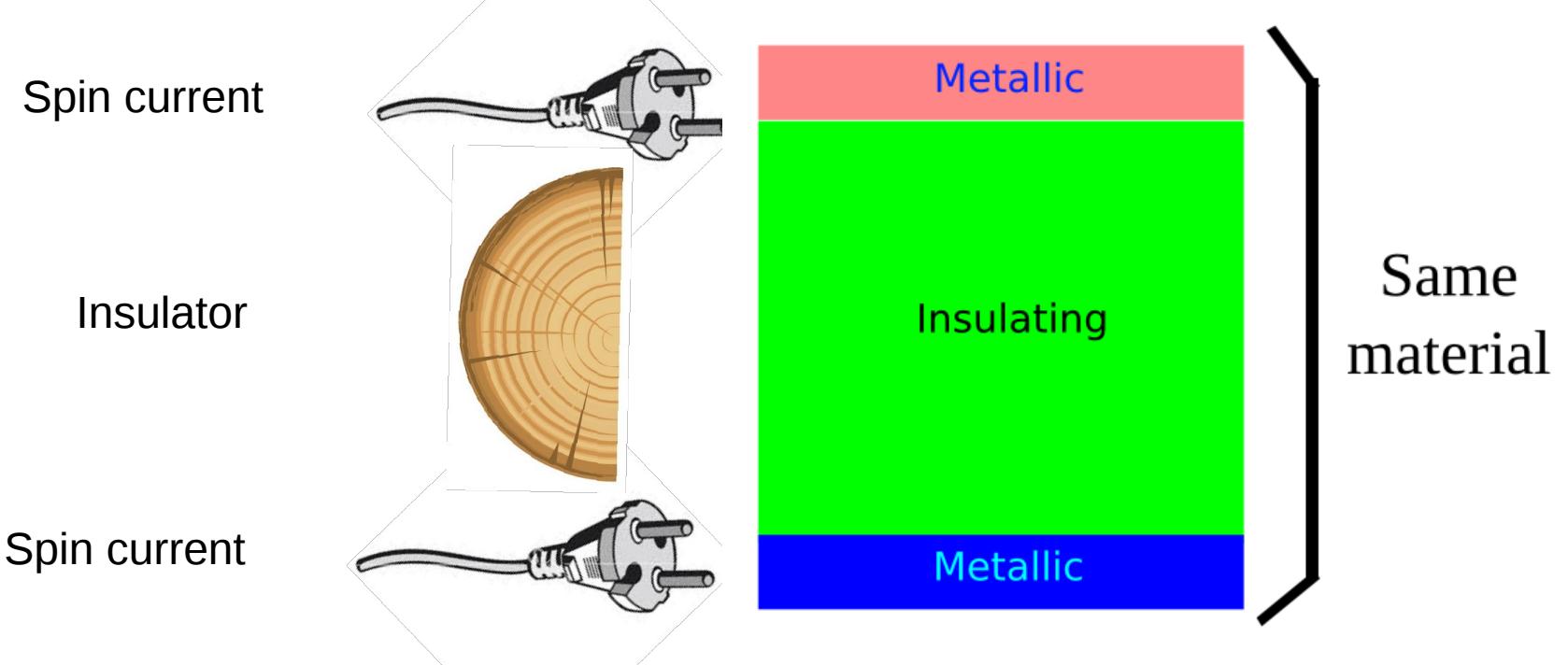


Jose Lado

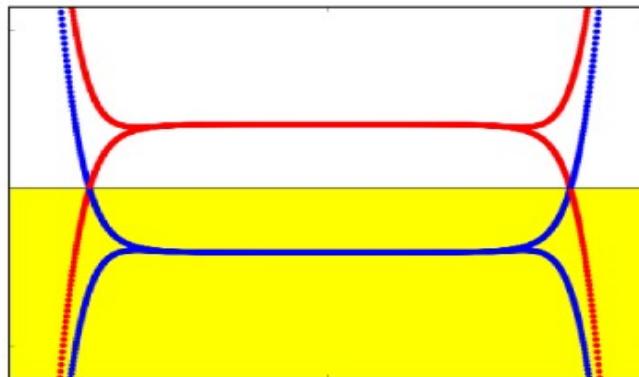
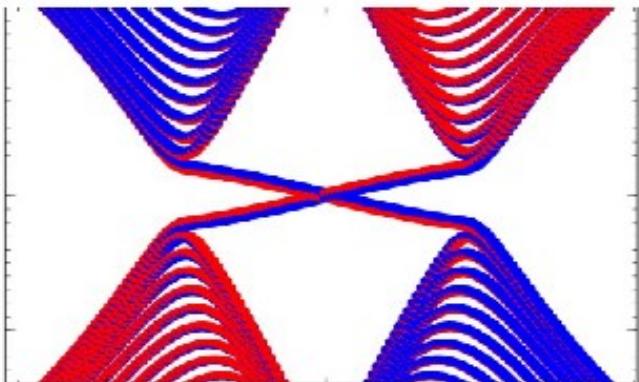


Joaquin
Rossier

Quantum Spin Hall



Quantum Spin Hall in graphene



\mathbb{Z}_2 topological insulator

Theory

Kane Mele PRL (2005)

Experiment

?????????



Spin Chern insulator

Theory

Abanin et al, PRL (2006)

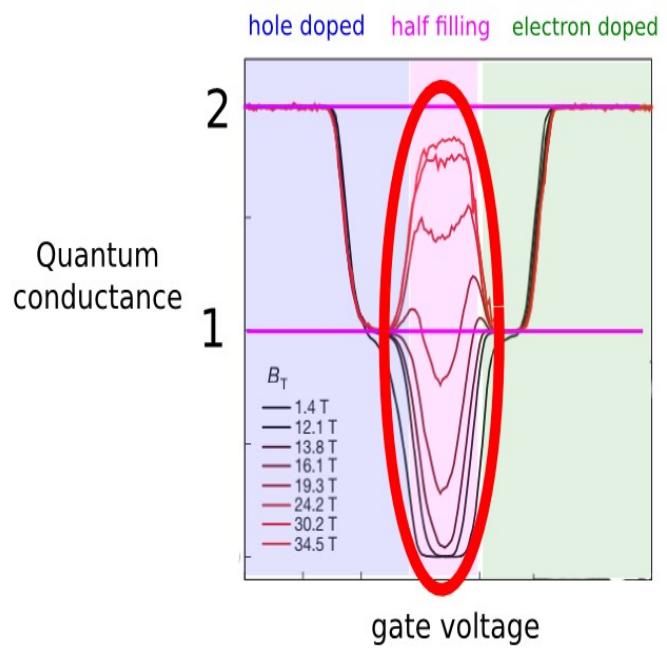
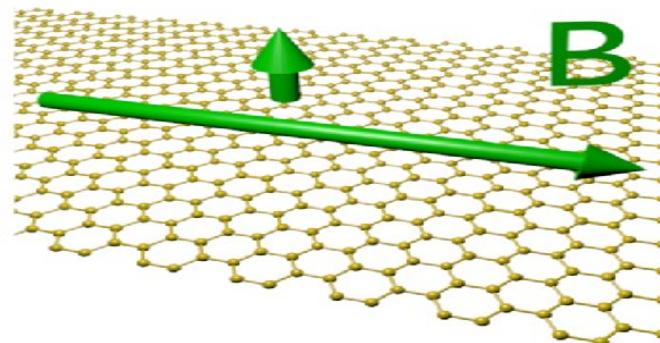
Experiment

A. F. Young et al, Nature (2014)

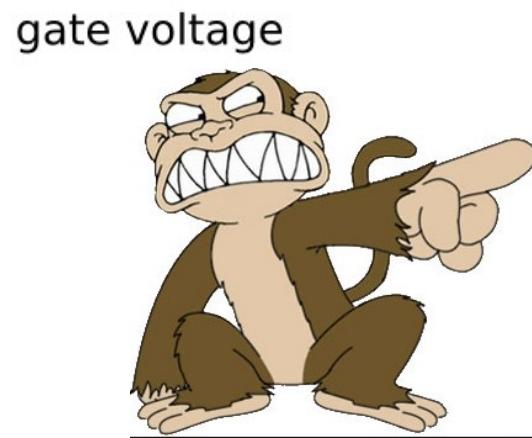
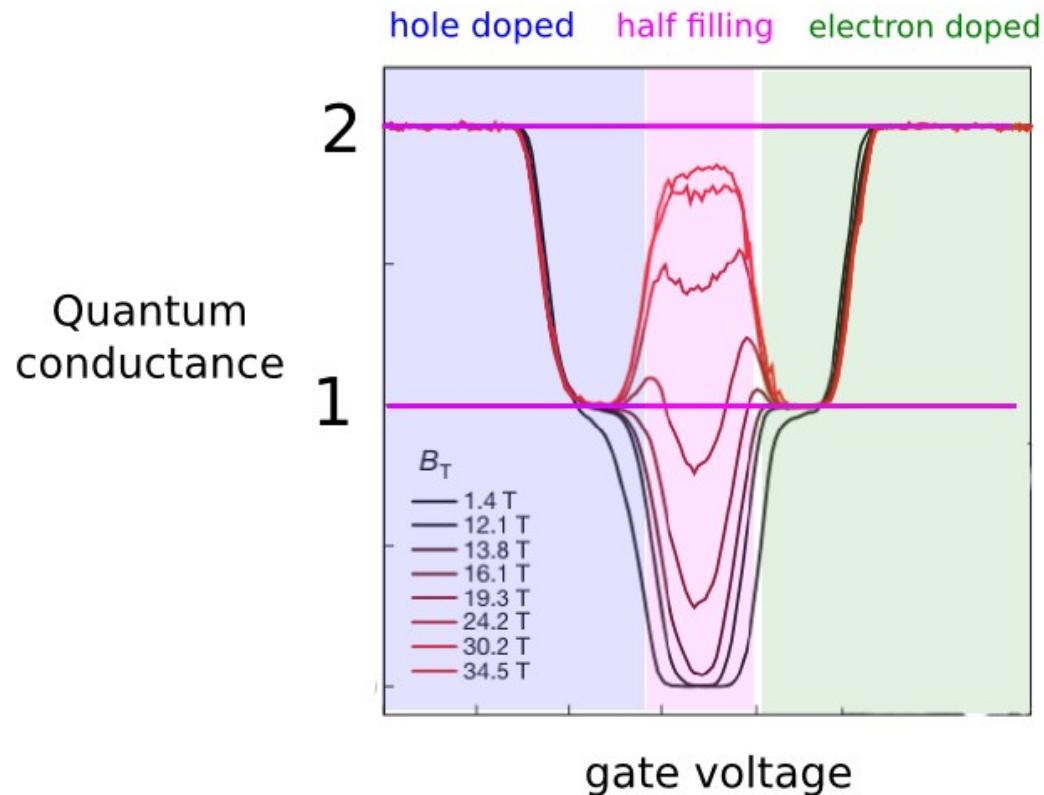
The experimental set-up

- High quality graphene
- Off-plane magnetic field
- In-plane magnetic field
- Variable doping via gate

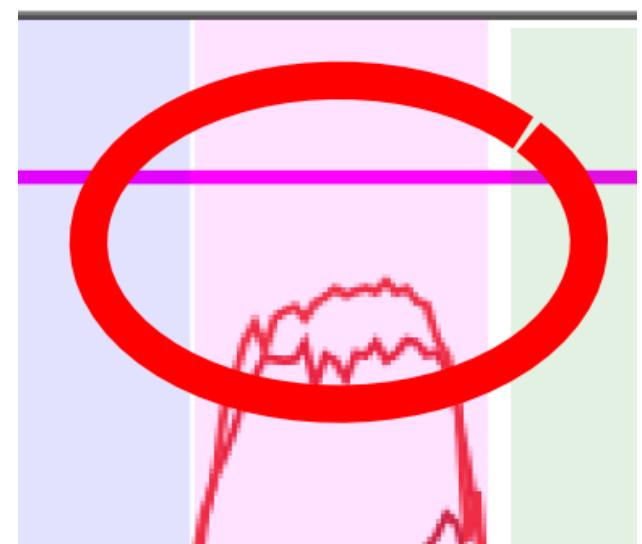
A. F. Young et al, *Nature* (2014)



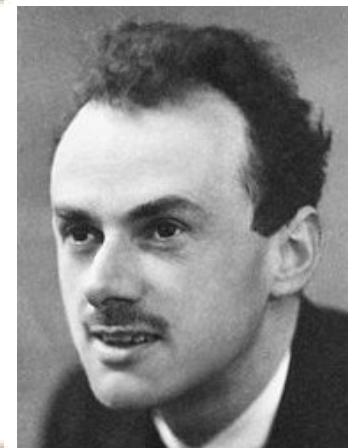
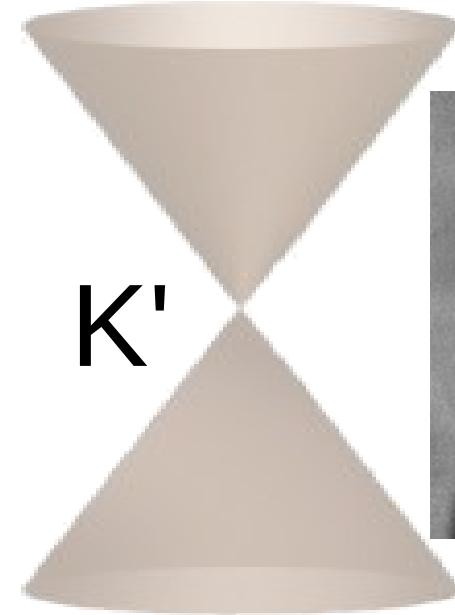
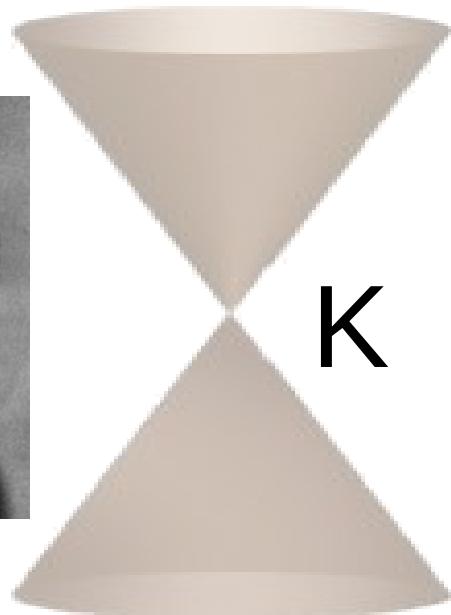
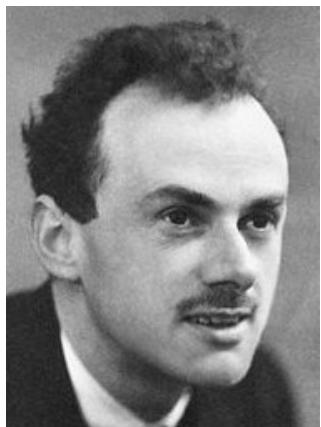
Not perfect conductance???



half filling



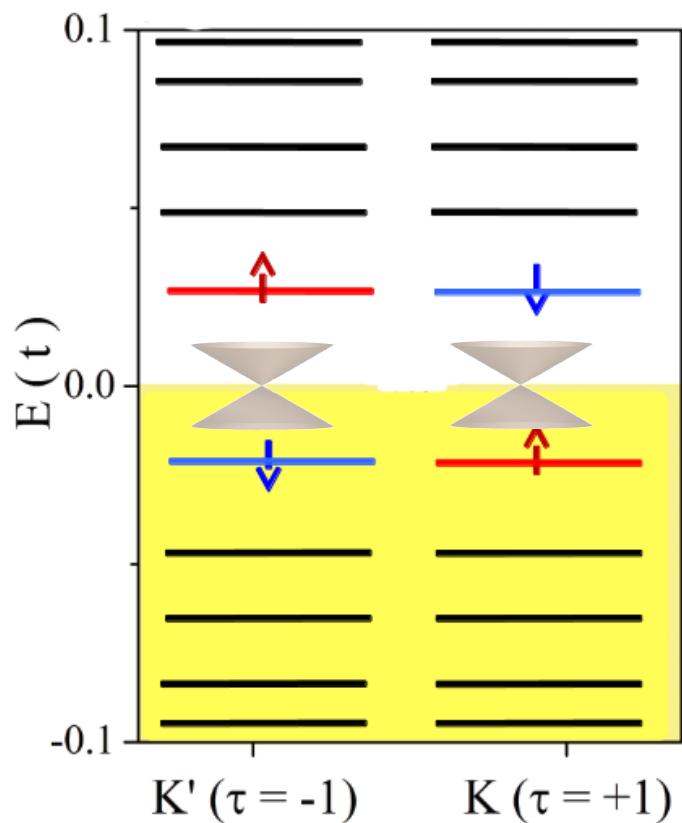
Low energy Hamiltonian



Two Dirac equations

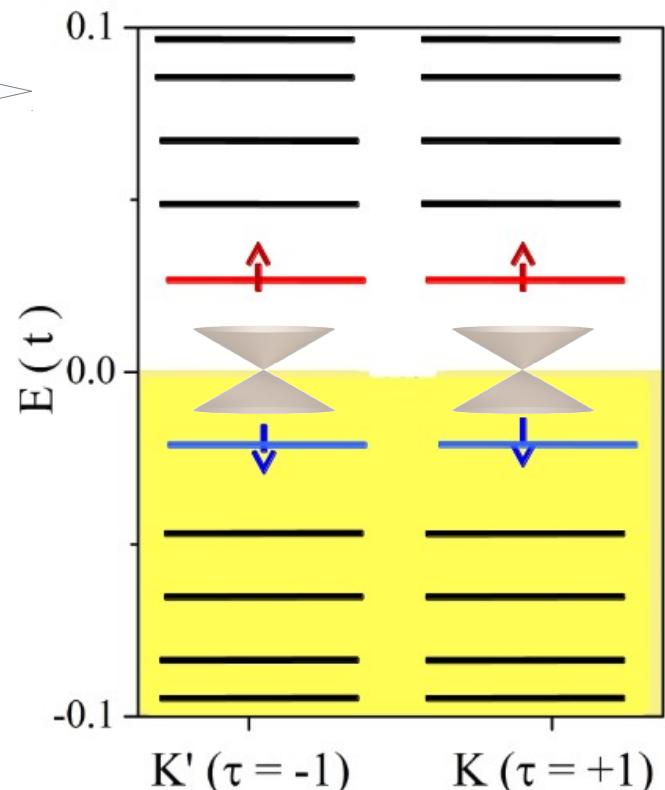
The Landau level picture

Antiferromagnetic



Spin Chern number = 0

Ferromagnetic

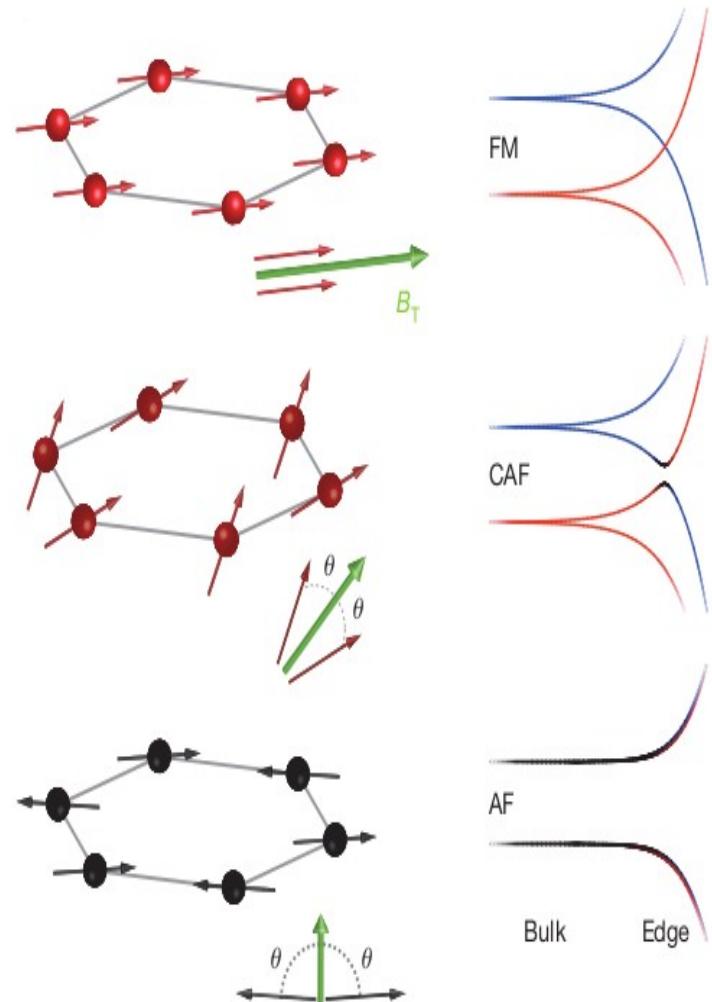
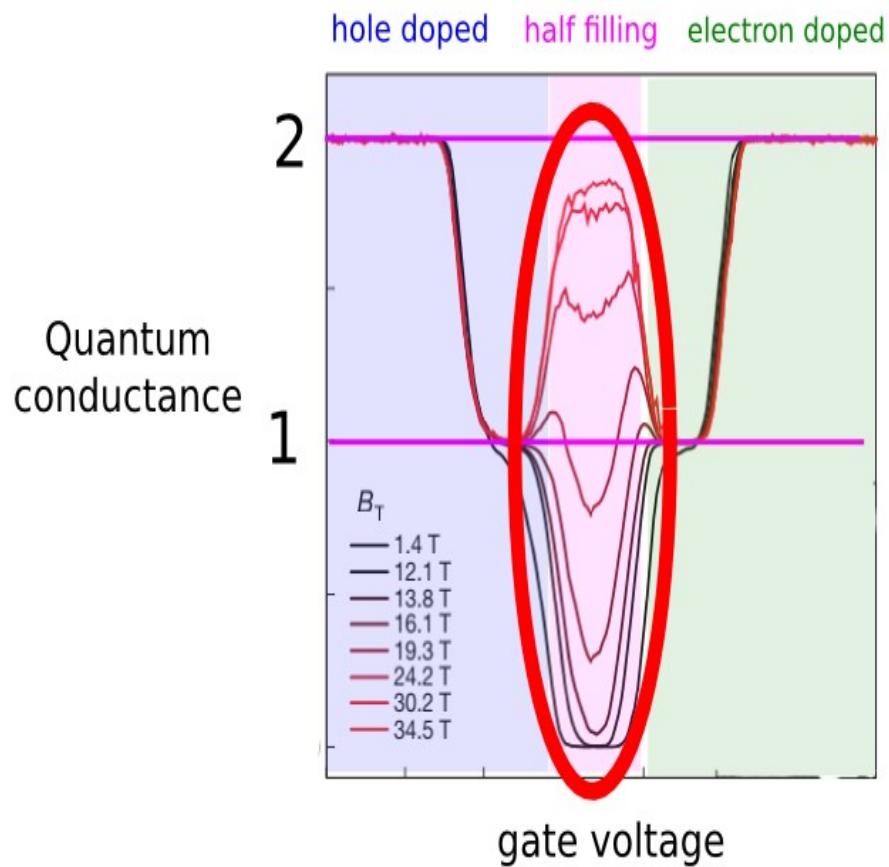


Spin Chern number = 2

Abanin et al, PRL (2006)

Increasing
Zeeman

Canted magnetism



A. F. Young et al, Nature (2014)

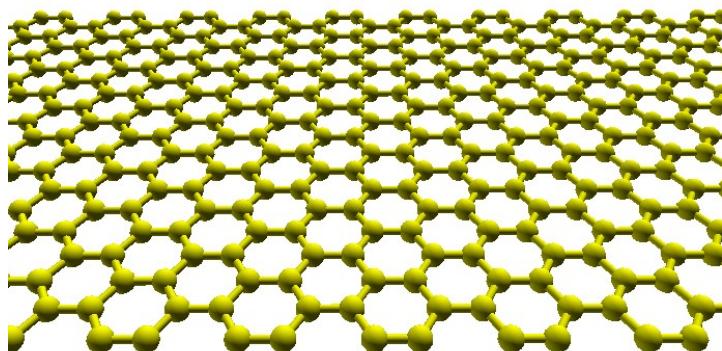
One ring model to rule them all

$$\mathcal{H} = \mathcal{H}_0(B_z) + g\mu_B \vec{B} \cdot \vec{S} + U \sum_i n_{i,\uparrow} n_{i,\downarrow}$$

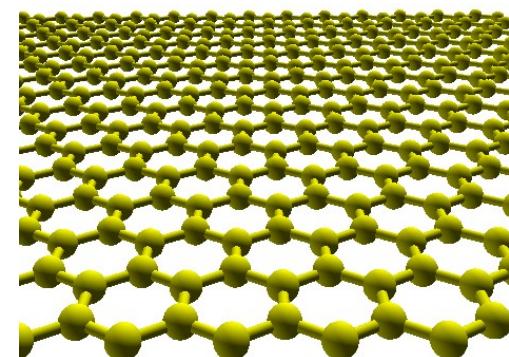
spin Zeeman field

nearest neighbor hopping
(with Peierls phase)

local e-e interaction
(Hubbard like)



ribbon geometry



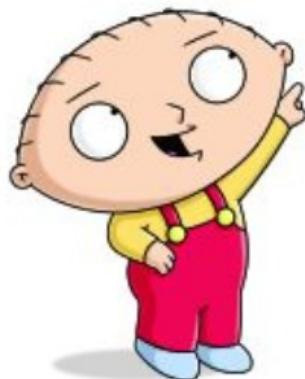
Solving the model

$$\mathcal{H} = \mathcal{H}_0(B_z) + g\mu_B \vec{B} \cdot \vec{S} + U \sum_i n_{i,\uparrow} n_{i,\downarrow}$$

Mean field antsaz

$$H^{MF} = H_0 + g\mu_B \vec{B} \cdot \vec{S} + H_H + H_F + E_{DC}$$

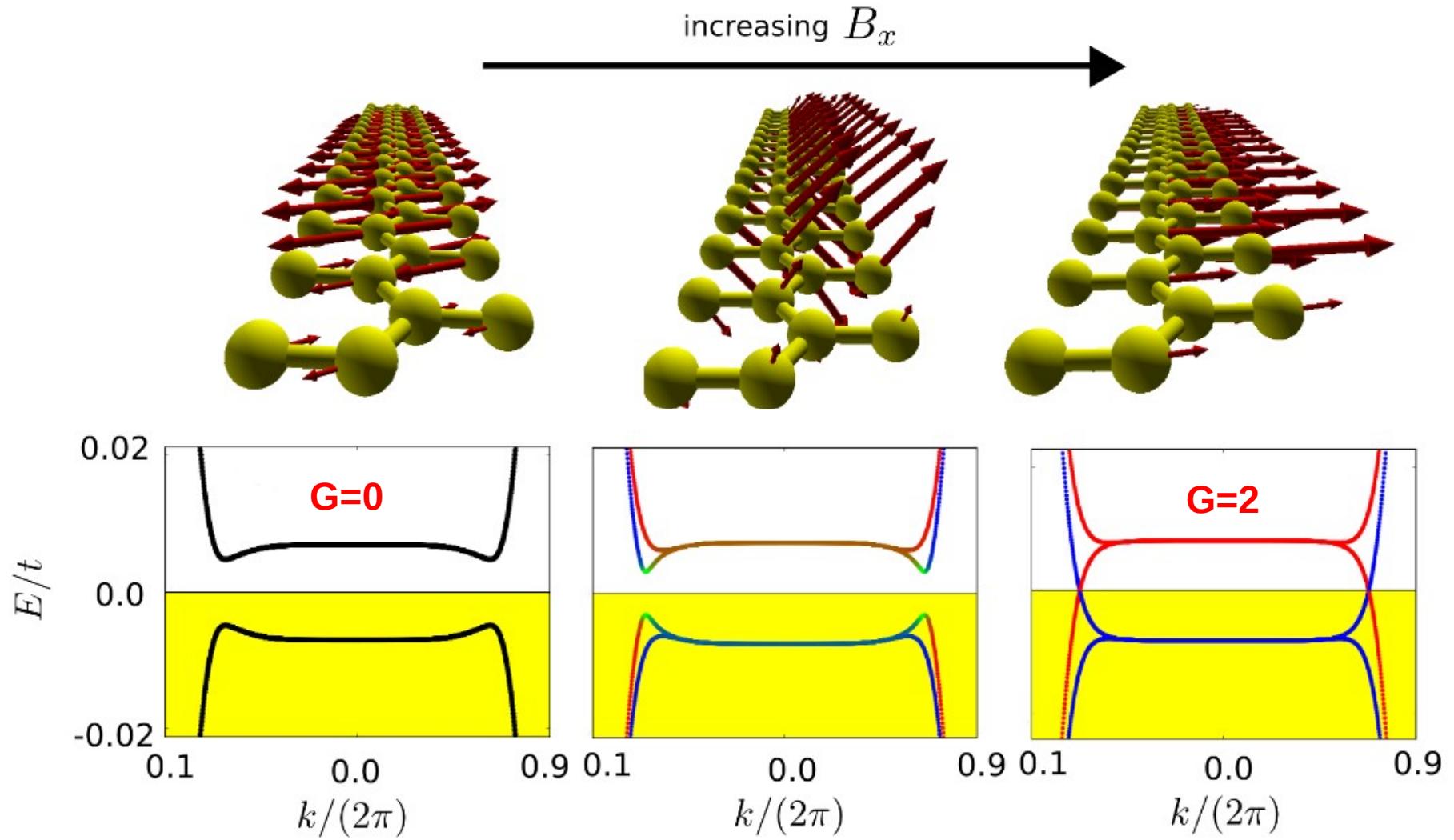
Collinear (Hartree) Exchange (Fock) Double counting



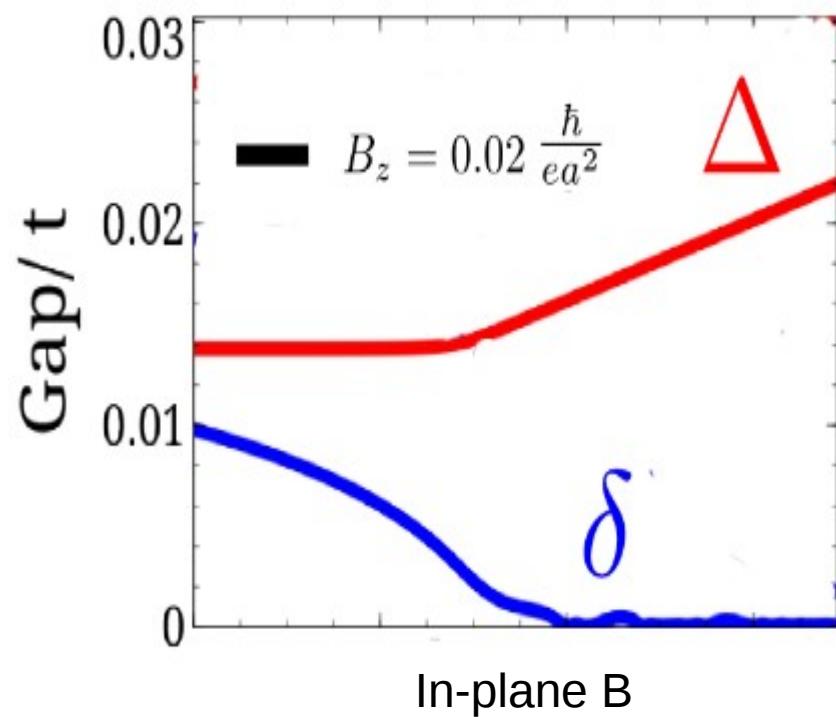
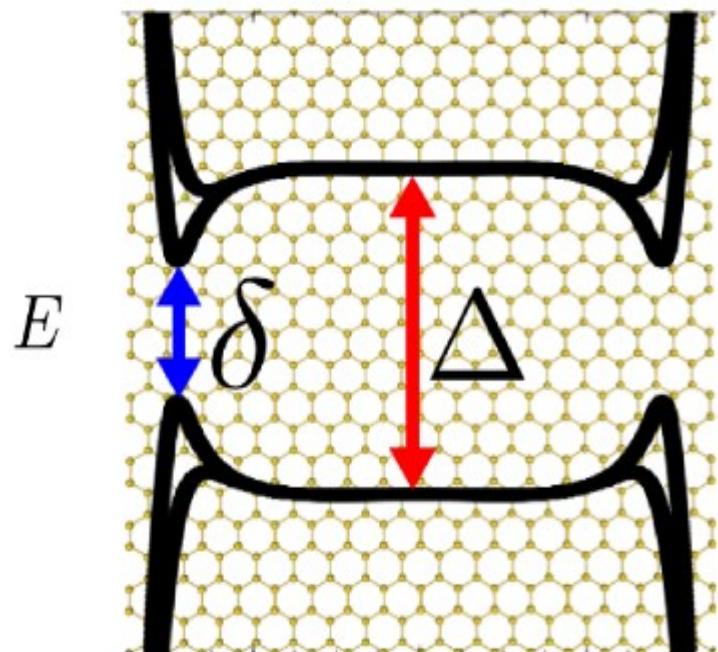
Variational wave function

$$|\Omega\rangle = \prod_i (u_i c_{i\uparrow}^\dagger + v_i c_{i\downarrow}^\dagger) |0\rangle$$

Transition at half filling with B_x



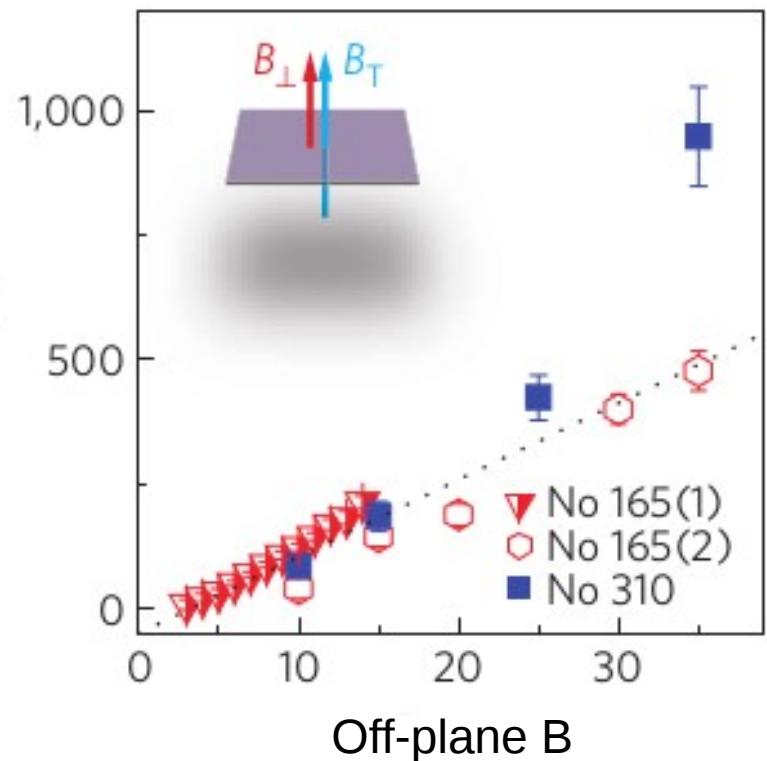
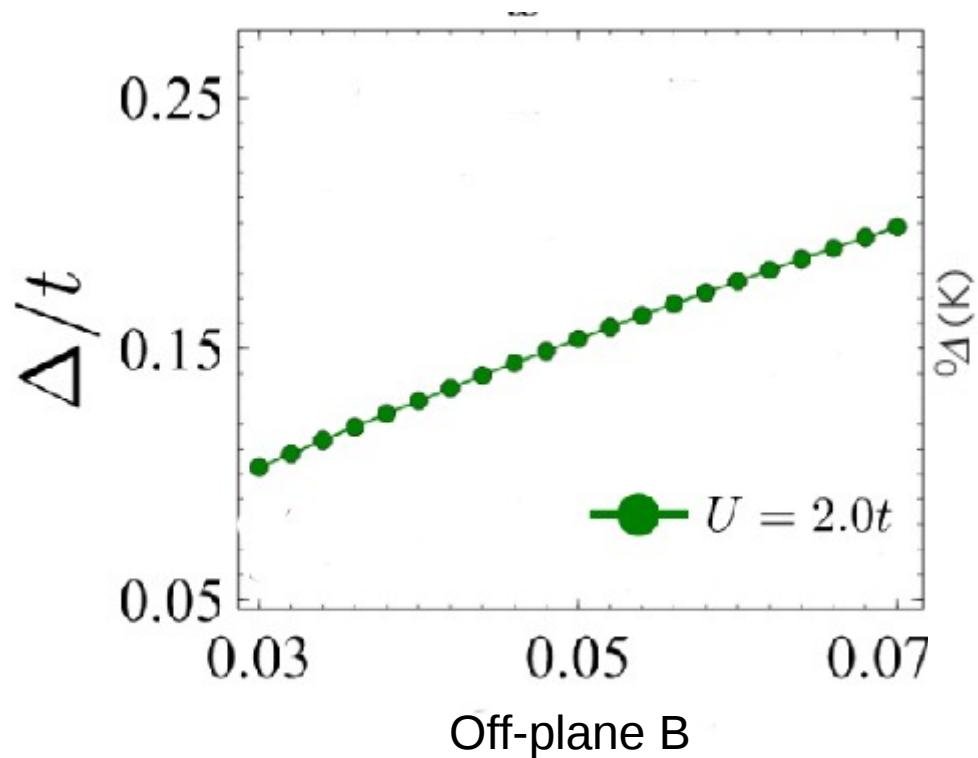
Transition at half filling with B_x



Only possible in the non-collinear formalism

Gap increases at half filling

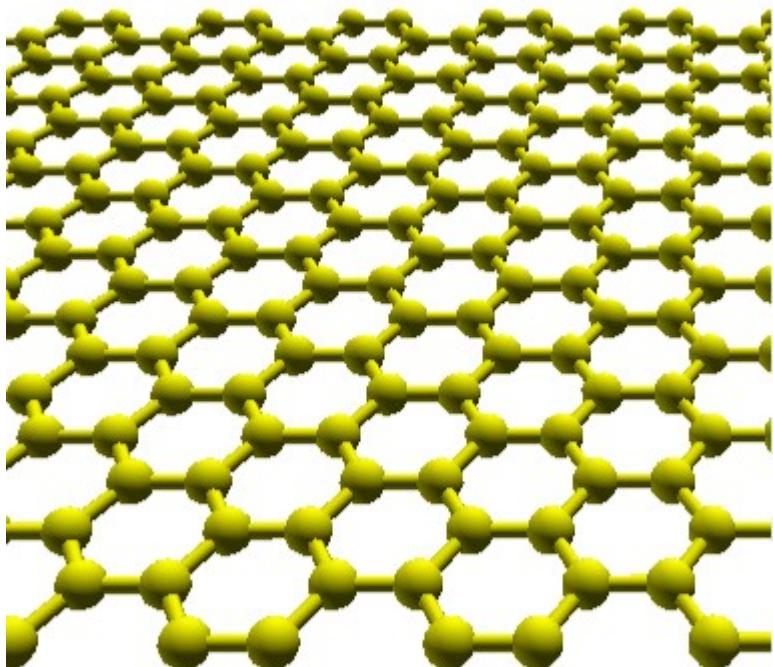
Hubbard model



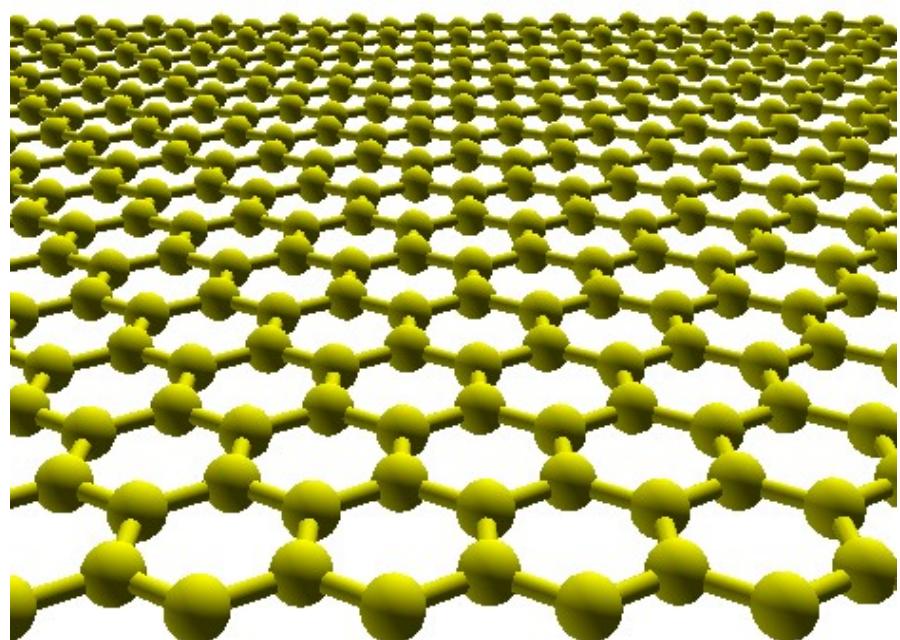
Gap increases linearly with off-plane field

Different edges

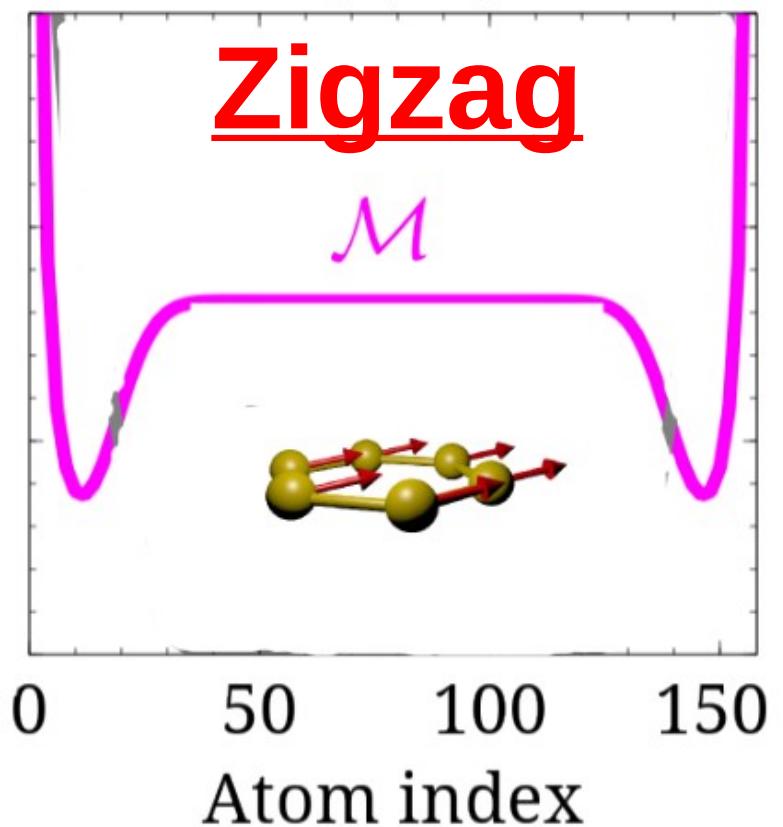
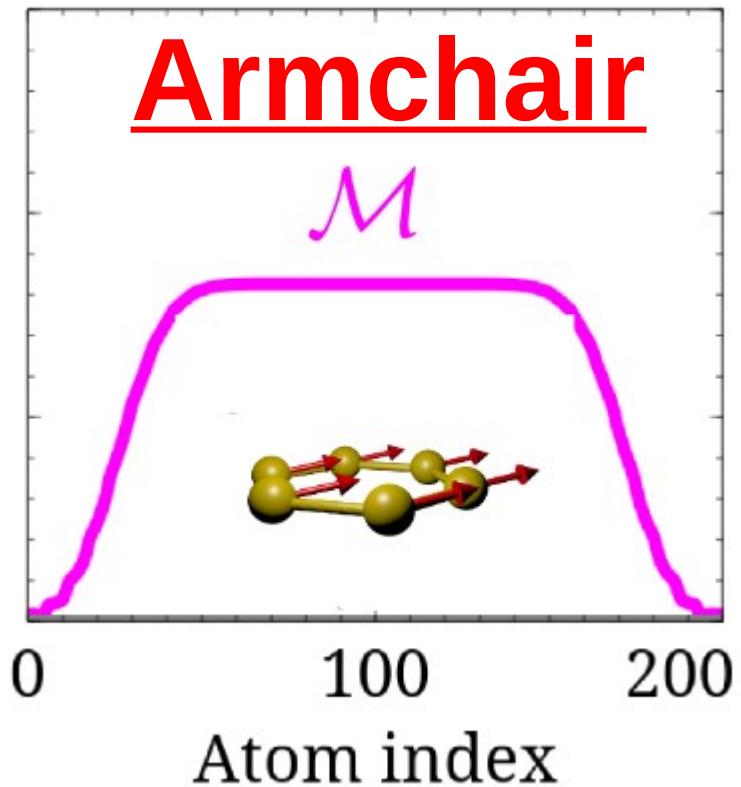
Armchair



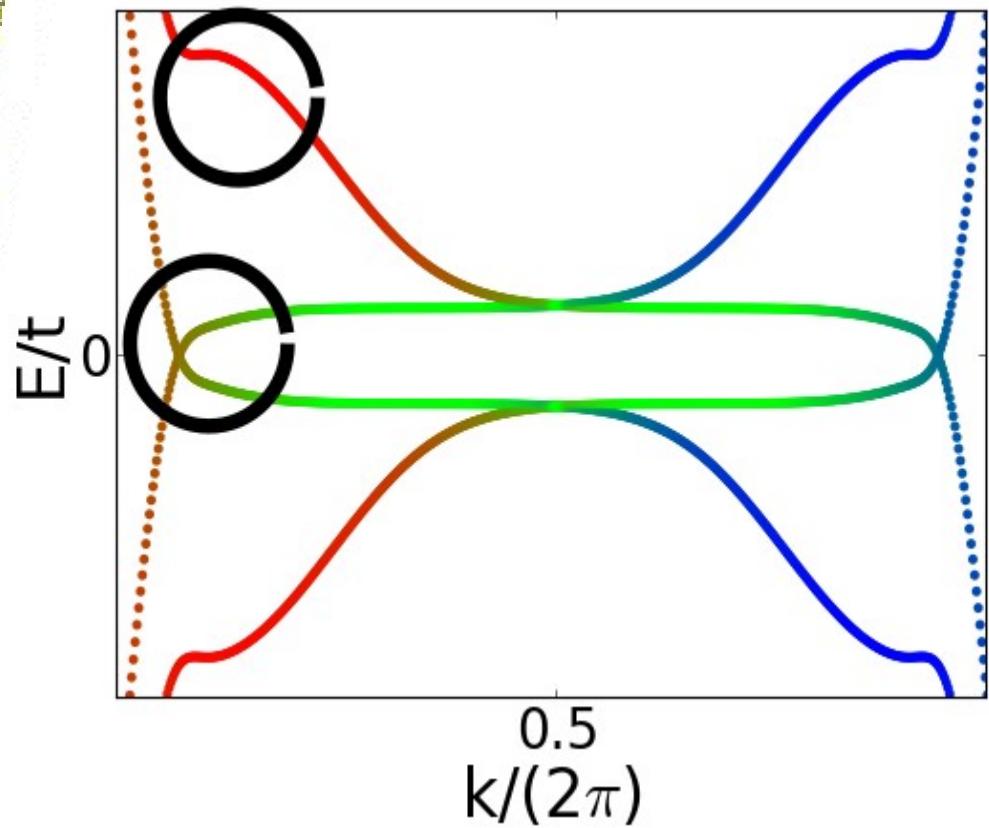
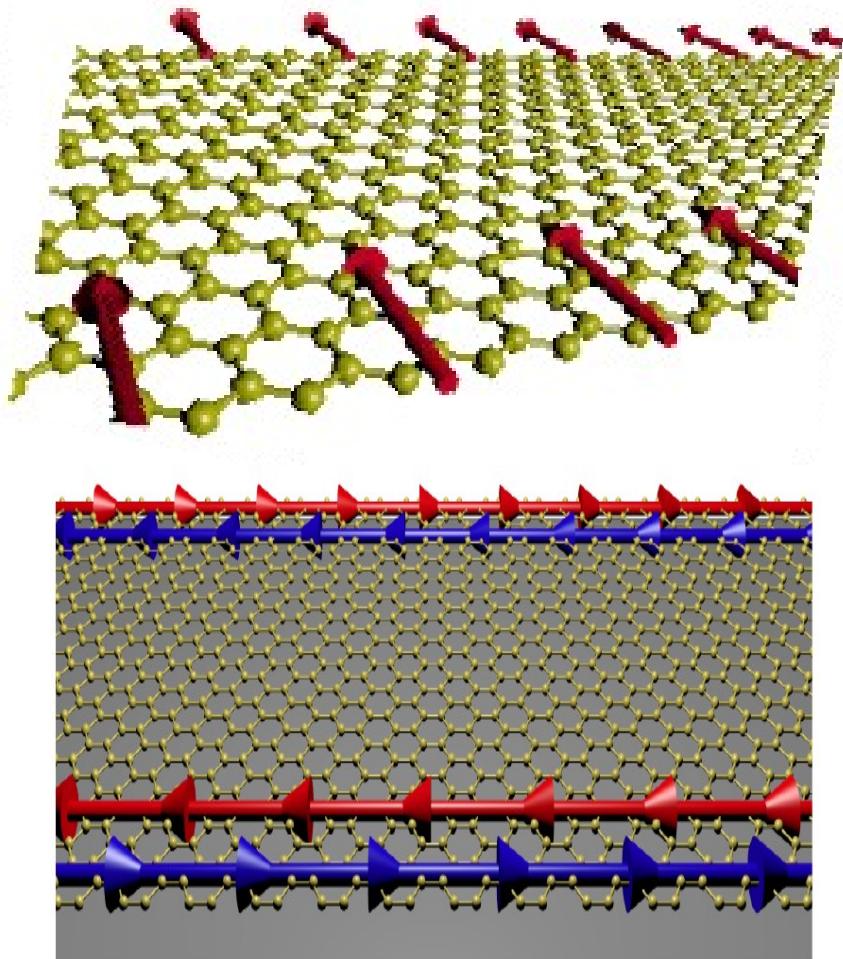
Zigzag



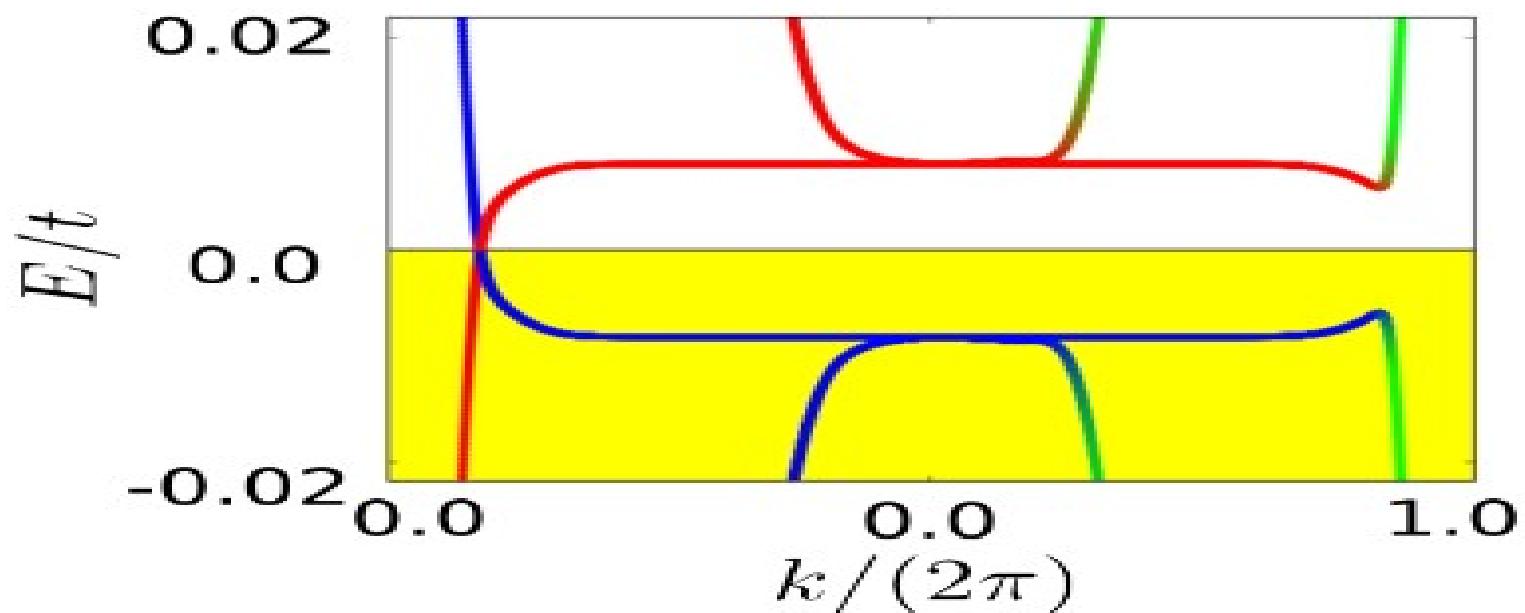
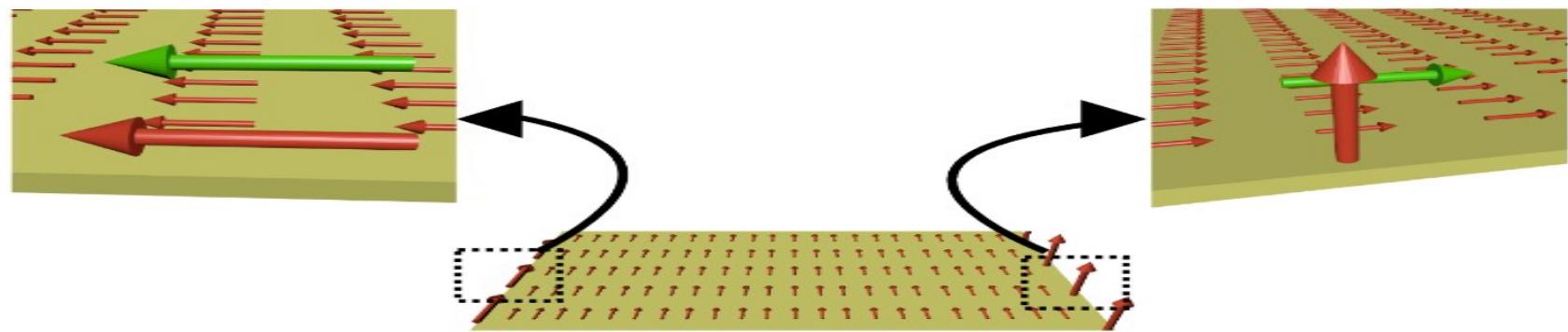
Edge dependent magnetism



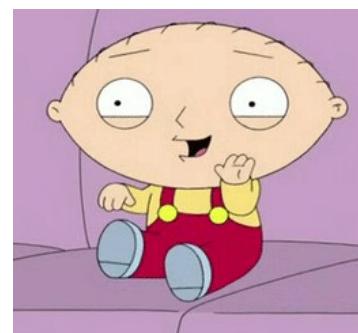
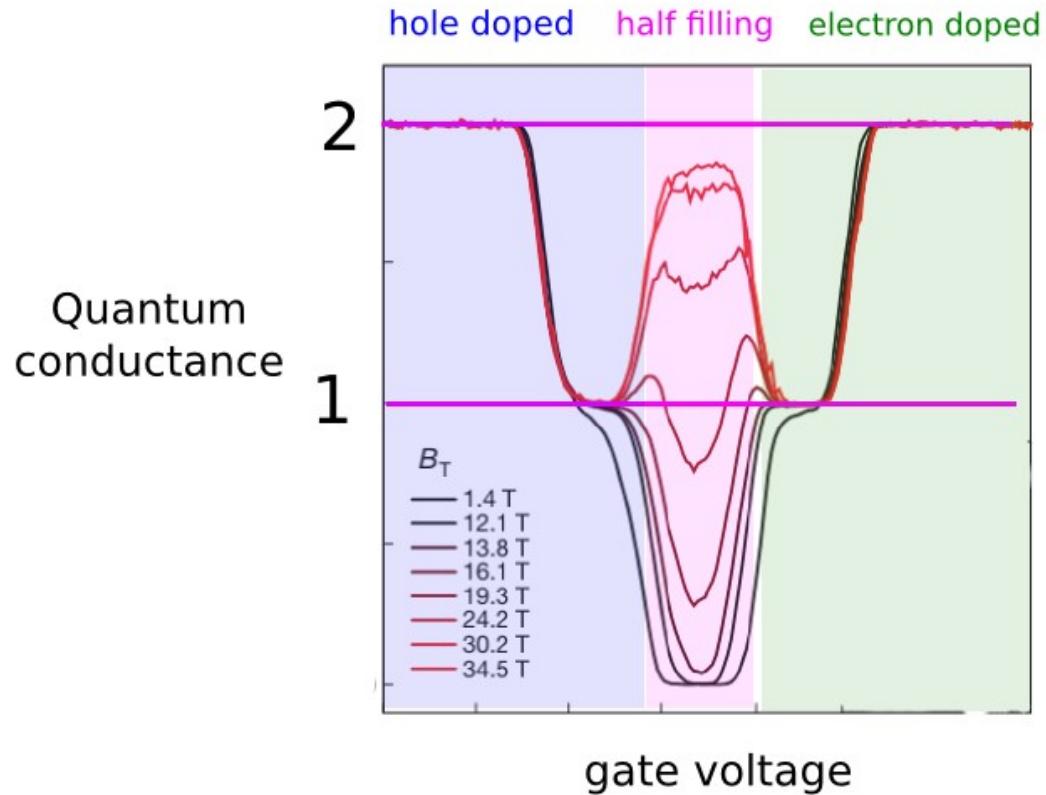
Two different edge states



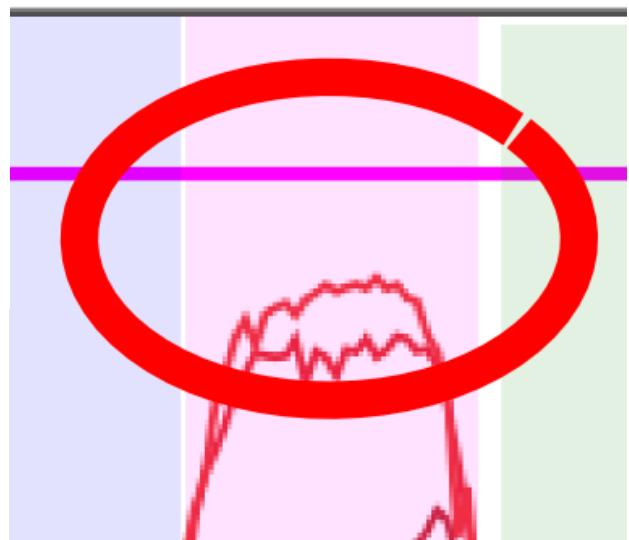
Electron-magnon coupling



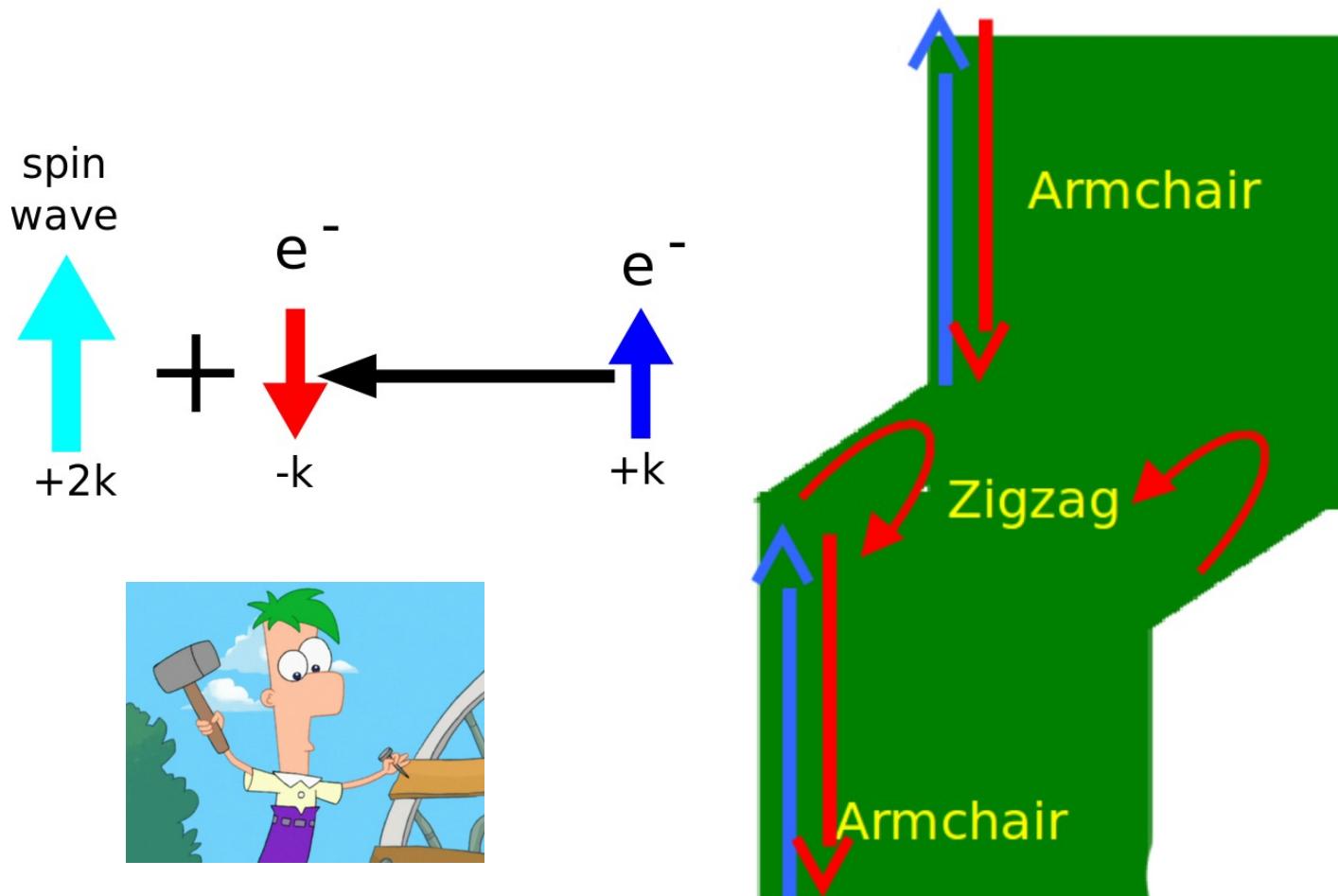
Back scattering channel



half filling



Mixed edges



Backscattering channel in zigzag part

Take home

- Interaction of different edge states opens up a channel for backscattering

But before finishing...

Funded by



Thank you!!!